南京大学 ACM-ICPC 集训队
calabash_boy
代码模版库

目录

1 String

1.1 Hash

```
427e // Created by calabash_boy on 18-6-1.
427e // CF 1003F
302f #include<bits/stdc++.h>
421c using namespace std;
b773 typedef unsigned long long ULL;
93c3 const int maxn = 305*305;
75c0 /* 字符集大小 */
0852 const int sigma = maxn;
0338 /* hash次数 */
cab3 const int HASH_CNT = 2;
5c83 int n;
4c95 int s[maxn];
bef3  /* char* 1-bas
5cb4  * sum[i] = s[i]+s[i-1]*Seed+s[i-2]*Seed^2+...+s[1]*Seed^(i-1)*/
cf6f ULL Prime_Pool[] = {1998585857ul,23333333333ul};
d095 ULL Seed_Pool[]={911,146527,19260817,91815541};
c437 ULL Mod_Pool[]={29123,998244353,1000000009,4294967291ull};
b060 struct Hash_1D{
3e0c     ULL Seed,Mod;
3bc4     ULL bas[maxn];ULL sum[maxn];
ad94     int perm[sigma];
be03     void init(int seedIndex,int modIndex){
e7a7         Seed = Seed_Pool[seedIndex];
53c7         Mod = Mod_Pool[modIndex];
bf6d         bas[0]=1;
6dbf         for (int i=1;i<=n;i++){
d57c             bas[i] = bas[i-1]*Seed%Mod;
95cf         }
6dbf         for (int i=1;i<=n;i++){
1e15             sum[i] = (sum[i-1]*Seed%Mod+s[i])%Mod;
95cf         }
95cf     }
c2c1     /*random_shuffle 离散化id，防止kill_hash*/
b864     void indexInit(int seedIndex,int modIndex){
324a         for (int i=1;i<n;i++){
871a             perm[i]=i;
95cf         }
cee0         random_shuffle(perm+1,perm+1+sigma);
e7a7         Seed = Seed_Pool[seedIndex];
53c7         Mod = Mod_Pool[modIndex];
bf6d         bas[0]=1;
6dbf         for (int i=1;i<=n;i++){
d57c             bas[i] = bas[i-1]*Seed%Mod;
95cf         }
6dbf         for (int i=1;i<=n;i++){
cd52             sum[i] = (sum[i-1]*Seed%Mod+perm[s[i]])%Mod;
95cf         }
95cf     }
b2c3     ULL getHash(int l,int r){
46bc         return (sum[r]-sum[l-1]*bas[r-l+1]%Mod+Mod)%Mod;
95cf     }
bb59 }hasher[HASH_CNT];
f09b map<pair<pair<ULL,ULL>,int>,int>veid;int vecnt;
5d53 map<string,int>id;int idcnt;
7fbd vector<int> pos[maxn];
fae2 string a[maxn];
f06b int sumL[maxn];
3117 int main(){
e1b6     cin>>n;
6dbf     for (int i=1;i<=n;i++){
879c         cin>>a[i];
d0a8         if (!id[a[i]])id[a[i]] = ++idcnt;
7798         s[i] = id[a[i]];
9892         sumL[i] = sumL[i-1]+a[i].size();
95cf     }
da02     for (int i=0;i<HASH_CNT;i++){
42fc         hasher[i].indexInit(i,i);
95cf     }
b20c     int ans = sumL[n]+n-1;
6dbf     for (int i=1;i<=n;i++){
ede7         for (int j=1;j<=n;j++){
e9bb             ULL hash1 = hasher[0].getHash(i,j);
2a70             ULL hash2 = hasher[1].getHash(i,j);
de4a             int len = j-i+1;
46fa             pair<pair<ULL,ULL>,int> x = {{hash1,hash2},len};
67ca             if (veid[x]==0)veid[x] = ++vecnt;
2251             pos[veid[x]].push_back(i);
95cf         }
95cf     }
04c1     int maxDelta =0;
0086     for (auto x:veid){
5c1e         int len = x.first.second;
76c1         int i = x.second;
```

```
3492        sort(pos[i].begin(),pos[i].end());
978f        int num =0;
6866        for (int j=0,last = -maxn;j<pos[i].size();j++){
683e            if (pos[i][j]>=last+len){
56e2                last = pos[i][j];
ac46                num++;
95cf            }
95cf        }
162f        if (num==1)continue;
e8b3        int cost1 = sumL[pos[i][0]+len-1]-sumL[pos[i][0]-1]+len-1;
939d        int cost2 = len;
5770        int tempDelta = (cost1-cost2)*num;
7f18        maxDelta = max(maxDelta,tempDelta);
95cf    }
cce6    cout<<ans-maxDelta<<endl;
7021    return 0;
95cf}
```

1.2 KMP

```
427e// Created by calabash_boy on 18-7-23.
427e//最小权值和 二维循环节
427e//找到最小 每行公共循环节+每列公共循环节。
427e//单调队列找固定大小矩形最小权值和。
302f#include<bits/stdc++.h>
421cusing namespace std;
94a1const int maxn = 1e6+100;
a239struct KMP{
8323    int nxt[maxn];int len;
0409    char t[maxn];
1126    void clear(){
3c88        len =nxt[0] = nxt[1] =0;
95cf    }
c0bf    /* 1-bas */
b115    /* 注意在ss结尾添加 '\0' */
2e3f    void init(char* ss){
64a4        len = strlen(ss+1);
b596        memcpy(t,ss,(len+2)*sizeof(char));
ca76        for (int i=2;i<=len;i++){
362a            nxt[i] = nxt[i-1];
bbb0            while (nxt[i]&&ss[i]!=ss[nxt[i]+1]) nxt[i] = nxt[nxt[i]];
da9f            nxt[i]+=(ss[i]==ss[nxt[i]+1]);
95cf        }
95cf    }
95cf}
49e0/* 求所有在ss串中的start_pos. 如果first_only设置为true，则只返回第一个位置*/
5cfdvector<int> match(char *ss,bool first_only = false){
55fa    int len_s = strlen(ss+1);
8364    vector<int> start_pos(0);
d287    for (int i=1,j=1;i<=len_s;){
8957        while (j!=1 && ss[i] != t[j])j = nxt[j-1]+1;
517c        if (ss[i] == t[j]) j++,i++;
aabb        else i++;
ffa2        if (j == len+1){
741d            start_pos.push_back(i-j+1);
f056            if (first_only)return start_pos;
d0e6            j = nxt[len]+1;
95cf        }
95cf    }
17e3    return start_pos;
95cf}
56ddvoid debug(){
0d69    for (int i=0;i<=len;i++){
3cb0        printf("[debug] nxt[%d]=%d\n",i,nxt[i]);
95cf    }
95cf}
243b/* 循环周期 形如 acaca 中 ac 是一个合法周期 */
d4e9vector<int> periodic(){
995a    vector<int> ret;
4a5d    int now = len;
3f78    while (now){
ebeb        now = nxt[now];
9341        ret.push_back(len-now);
95cf    }
ee0f    return ret;
95cf}
f525/* 循环节 形如 acac 中ac、acac是循环节，aca不是*/
1a85vector<int> periodic_loop(){
995a    vector<int>ret ;
d561    for (int x :periodic()){
901d        if (len%x==0)ret.push_back(x);
95cf    }
ee0f    return ret;
95cf}
5531int min_periodic_loop(){
8b2c    return periodic_loop()[0];
95cf}
```

```
}kmper;
vector<string> s;
vector<vector<int> > a,maxVal;
int cnt1[maxn],cnt2[maxn],n,m;
char S[maxn];
pair<int,int> pq[maxn];int l,r;
int main(){
    cin>>n>>m;
    s.resize(n+1);
    maxVal.resize(n+1);
    for (int i=1; i<=n;i++){
        cin>>s[i];
    }
    a.resize(n+1);
    for (int i=1;i<=n;i++){
        a[i].resize(m+1);
        maxVal[i].resize(m+1);
        for (int j=1;j<=m;j++){
            cin>>a[i][j];
        }
    }
    int p,q;kmper.clear();
    for (int i=1;i<=n;i++){
        for (int j=1;j<=m;j++){
            S[j] = s[i][j-1];
        }
        S[m+1]='\0';
        kmper.init(S);
        for (int x:kmper.periodic()){
            cnt1[x]++;
        }
    }
    for (int j=1;j<=m;j++){
        for (int i=1;i<=n;i++){
            S[i] = s[i][j-1];
        }
        S[n+1]='\0';
        kmper.init(S);
        for (int x:kmper.periodic()){
            cnt2[x]++;
        }
    }
    for (int i=maxn;i>=1;i--){
        if (cnt1[i]==n){ q = i; }
        if (cnt2[i]==m){ p=i; }
    }
    for (int i=1;i<=n;i++){
        l = 0,r=0;
        for (int j=1;j<=m;j++){
            while (r>l&&pq[l].second<=j-q)l++;
            while (r>l&&pq[r-1].first<=a[i][j])r--;
            pq[r++] = {a[i][j],j};
            if (j>=q){
                maxVal[i][j-q+1] = pq[l].first;
            }
        }
    }
    int ans = 0x3f3f3f3f;
    for (int j=1;j<=m-q+1;j++){
        l=r=0;
        for (int i=1;i<=n;i++){
            while (r>l&&pq[l].second<=i-p)l++;
            while (r>l&&pq[r-1].first<=maxVal[i][j])r--;
            pq[r++] = {maxVal[i][j],i};
            if (i>=p){
                ans = min(ans,pq[l].first);
            }

        }
    }
    cout<<1LL*(p+1)*(q+1)*ans<<endl;
    return 0;
}
```

1.3 EX KMP

```
// Created by calabash_boy on 2019/12/11.
// CF 1200E
#include <bits/stdc++.h>
using namespace std;
const int maxn = 1e6 + 100;
//result: extend[i] = LCP(S[i,lens],T)
//require: nxt[i] = LCP(T[i,lent],T)
void exkmp(char *s,int lens,char *t,int lent,int *extend,int *nxt){
    extend[0] = 0;
    for (int i = 1,p0 = 0,p = 0;i <= lens;i ++){
```

```
c132        extend[i] = i <= p ? min(nxt[i - p0 + 1], p - i + 1) : 0;
d4c2        while (i + extend[i] <= lens and extend[i] < lent and s[i + extend[i]]
              == t[extend[i]+1])extend[i] ++;
cc3f        if (i + extend[i] - 1 >= p and i != 1)p0 = i,p = i + extend[i] - 1;
95cf    }
95cf }
8304 char s[maxn],t[maxn];
bbbc int extend[maxn];
51d9 int nxt[maxn];
3117 int main(){
5c83    int n;
cd91    scanf("%d",&n);
9f73    int LEN = 0;
6dbf    for (int i=1;i<=n;i++){
79ca        scanf("%s",t+1);
be5a        int lent = strlen(t+1);
f312        int lens = min(LEN,lent);
0640        exkmp(t,lent,t,lent,nxt,nxt);
b881        exkmp(s + LEN - lens,lens,t,lent,extend,nxt);
eb16        int sp = 0;
0d89        for (int j = 1;j <= lens;j ++){
80e7            if (lens - j + 1 == extend[j]){
fa6b                sp = extend[j];
6173                break;
95cf            }
95cf        }
1e32        strcpy(s + LEN+1,t + sp + 1);
df1b        LEN += lent - sp;
95cf    }
ae85    printf("%s\n",s+1);
7021    return 0;
95cf }
```

1.4 Manacher

```
427e // Created by calabash_boy on 18-9-14.
302f #include<bits/stdc++.h>
421c using namespace std;
571f const int MAX = 2e5+10000;
99d0 char s[MAX];
81d4 struct Manacher{
9ccd    char ch[MAX];                                                    04f3
d7af    int N;                                                           d7af
053c    Manacher(char *s){init(s);manacher();}                           053c
44ca    /* s 1 bas */                                                    44ca
e798    void init(char *s){                                              e798
0de8        int n = strlen(s+1);                                         0de8
ad19        ch[n*2 +1] = '#';                                            ad19
ce0d        ch[0] = '@';                                                 ce0d
46cd        ch[n*2 +2] = '\0';                                           46cd
0c3f        for (int i=n;i>=1;i--){                                      0c3f
6beb            ch[i*2] = s[i];ch[i*2 -1] = '#';                         6beb
95cf        }                                                            95cf
5991        N = 2* n +1;                                                 5991
95cf    }                                                                95cf
6c5f    void manacher(){                                                 6c5f
a461        lc[1]=1;  int k=1;                                           a461
256b        for (int i=2;i<=N;i++){                                      256b
7957            int p = k+lc[k]-1;                                       7957
5e04            if (i<=p){                                               5e04
24a1                lc[i]=min(lc[2*k-i],p-i+1);                          24a1
87d6            }else{  lc[i]=1;  }                                      87d6
aa80            while (ch[i+lc[i]]==ch[i-lc[i]])lc[i]++;                 aa80
2b9a            if (i+lc[i]>k+lc[k])k=i;                                 2b9a
95cf        }                                                            95cf
95cf    }                                                                95cf
56dd    void debug(){                                                    56dd
b492        puts(ch);                                                    b492
cd0f        for (int i=1;i<=N;i++){                                      cd0f
0d62            printf("lc[%d]=%d\n",i,lc[i]);                           0d62
95cf        }                                                            95cf
95cf    }                                                                95cf
329b };                                                                  329b
3117 int main(){                                                         3117
a275    scanf("%s",s+1);                                                 a275
382e    Manacher manacher(s);                                            382e
9c07    manacher.debug();                                                9c07
7021    return 0;                                                        7021
95cf }                                                                   95cf
```

1.5 Palindrome Series

```
427e // Created by calabash_boy on 19-11-20.                            427e
```

```
427e // CF 932G 偶回文分割方案数
427e // 优化DP转移：枚举所有回文后缀转移
427e // 使用时，只需要修改3行TBD
302f #include<bits/stdc++.h>
421c using namespace std;
5d33 const int mod = 1e9 + 7;
94a1 const int maxn = 1e6+100;
466b struct Palindromic_AutoMaton{
9f36     int s[maxn],now;
f801     int nxt[maxn][26],fail[maxn],l[maxn],last,tot;
7220     int diff[maxn],anc[maxn],g[maxn],f[maxn];
1126     void clear(){
427e         //1节点：奇数长度root 0节点：偶数长度root
78a6         s[0] = l[1] = -1;
b6d0         fail[0] = tot = now =1;
f40b         last = l[0] = 0;
21a1         memset(nxt[0],0,sizeof nxt[0]);
9b85         memset(nxt[1],0,sizeof nxt[1]);
95cf     }
61ff     Palindromic_AutoMaton(){clear();}
7c3e     int newnode(int len){
71cf         tot++;
87f4         memset(nxt[tot],0,sizeof nxt[tot]);
cdd3         fail[tot]=0;l[tot]=len;
91fb         return tot;
95cf     }
4284     int get_fail(int x){
8ef1         while (s[now-l[x]-2]!=s[now-1])x = fail[x];
d074         return x;
95cf     }
a791     void add(int ch){
3622         s[now++] = ch;
051b         int cur = get_fail(last);
a980         if(!nxt[cur][ch]){
80d2             int tt = newnode(l[cur]+2);
2f33             fail[tt] = nxt[get_fail(fail[cur])][ch];
01cb             nxt[cur][ch] = tt;
ba51             diff[tt] = l[tt] - l[fail[tt]];
9bbc             anc[tt] = diff[tt] == diff[fail[tt]]? anc[fail[tt]] : fail[tt];
95cf         }
4e23         last = nxt[cur][ch];
95cf     }
ea60     void trans(int i){
8380         for (int p = last;p>1;p = anc[p]){
2237             g[p] = f[i - l[anc[p]] - diff[p]];/*TBD*/
752d             if (diff[p] == diff[fail[p]]){
a45f                 (g[p] += g[fail[p]]) %= mod;/*TBD*/
95cf             }
4ae5             (f[i] += (i % 2 == 0) *g[p]) %= mod;/*TBD*/
95cf         }
95cf     }
01f2     int init(char* s){
0cac         f[0] = 1;
0de8         int n = strlen(s + 1);
6dbf         for (int i=1;i<=n;i++){
341e             add(s[i] - 'a');
271c             trans(i);
95cf         }
1df1         return f[n];
95cf     }
de71 }pam;
394b char t[maxn], s[maxn];
3117 int main(){
a275     scanf("%s",s + 1);
0de8     int n = strlen(s+1);
3966     for (int i=1;i<=n/2;i++){
45f1         t[2 * i - 1] = s[i];
d9af         t[2 * i] = s[n + 1- i ];
95cf     }
d348     cout<<pam.init(t)<<endl;
7021     return 0;
95cf }
```

1.6 Suffix Array

```
87e7 /*
1e1d  * for each 2-power string.
f606  * let its length is 2L. add edge of length w[L] between every i and i + L.
f3db  * calculate the spanning forests.
f2b5  */
302f #include <bits/stdc++.h>
18f5 #define rank rkrkrk
427e //#define _DEBUG
f11b #define RMQ
421c using namespace std;
6428 const int maxn = 3e5+100;
```

```
82ea int w[maxn];
1283 int lg[maxn];
2f33 struct Run{
8f36     int l,r,k;
329b };
bd89 struct UFS {
33ef     int fa[maxn];
7dd9     void init(int n) { iota(fa, fa + n + 1, 0); }
38dd     int find(int x) { return fa[x] == x ? x : fa[x] = find(fa[x]); }
9662     bool unite(int u, int v) {
576f         u = find(u); v = find(v);
2448         fa[u] = v;
4042         return u != v;
95cf     }
d71b } ufs[20];
427e
4d49 int unite(int u, int v, int k) {
10fe     if (ufs[k].unite(u, v)) {
d11e         if (k == 0) return 1;
81a9         return unite(u, v, k - 1) + unite(u + (1<<(k-1)), v + (1<<(k-1)), k - 1)
               ;
aad3     } else return 0;
95cf }
427e
6b2b long long merge(int u, int v, int l) {
0fa9     int k = log2(l);
2c46     int ret =  unite(u, v, k) +
270b                unite(u + l - (1<<k), v + l - (1<<k), k);
ee0f     return ret;
95cf }
3b88 struct SA{
4eb6 #ifndef RMQ
9c29     struct Segment_Tree{
77b7         int min_val[maxn*4];
d08d         void up(int x){
10d7             min_val[x] = min(min_val[x<<1],min_val[x<<1|1]);
95cf         }
3e01         void build(int x,int l,int r,int*h){
3a0d             if (l == r){
e948                 min_val[x] = h[l];
4f2d                 return;
95cf             }
b8b7             int mid = l + r >>1;
fdb0             build(x<<1,l,mid,h);
06e9             build(x<<1|1,mid+1,r,h);
cf00             up(x);
95cf         }
30b1         int query(int x,int l,int r,int L,int R){
133b             if (l > R || L > r)return 0x3f3f3f3f;
0739             if (L<= l && r <= R)return min_val[x];
b8b7             int mid = l + r >> 1;
edf8             return min(query(x<<1,l,mid,L,R),query(x<<1|1,mid+1,r,L,R));
95cf         }
f7fb     }segtree;
a8cb #else
fb7f     int st[maxn][20];
a66e     void st_init(int n,int*h){
6dbf         for (int i=1;i<=n;i++){
fc74             st[i][0] = h[i];
95cf         }
c8a2         for (int j=1;(1<<j)<=n;j++){
672f             for (int i=1;i<=n-(1<<j)+1;i++){
3c6e                 st[i][j] = min(st[i][j-1],st[i+(1<<(j-1))][j-1]);
95cf             }
95cf         }
95cf     }
1937 #endif
6e4f     int cntA[maxn],cntB[maxn],tsa[maxn],A[maxn],B[maxn];
f3d8     int sa[maxn],rank[maxn],height[maxn];
81e4     void get_sa(int * ch,int n){
b5cc         ch[0] = ch[n+1] = -1;
c7f9         for (int i=0;i<=n;i++)cntA[i] = 0;
e86b         for (int i=1;i<=n;i++)cntA[ch[i]]++;
c35a         for (int i=1;i<=n;i++)cntA[i] += cntA[i-1];
625e         for (int i=n;i>=1;i--)sa[cntA[ch[i]]--] = i;
c9f2         rank[sa[1]] = 1;
a5c5         for (int i=2;i<=n;i++){
dc5c             rank[sa[i]] = rank[sa[i-1]];
459c             if (ch[sa[i]] != ch[sa[i-1]])rank[sa[i]] ++;
95cf         }
f62b         for (int l=1;rank[sa[n]]<n;l<<=1){
c794             for (int i=0;i<=n;i++)cntA[i] = cntB[i] = 0;
6dbf             for (int i=1;i<=n;i++){
d9ab                 cntA[A[i] = rank[i]] ++;
c846                 cntB[B[i]=(i+l<=n)?rank[i+l]:0]++;
95cf             }
72d7             for (int i=1;i<=n;i++)cntB[i] += cntB[i-1];
4c62             for (int i=n;i>=1;i--)tsa[cntB[B[i]]--] = i;
```

```
c35a            for (int i=1;i<=n;i++)cntA[i] += cntA[i-1];
1626            for (int i=n;i>=1;i--)sa[cntA[A[tsa[i]]]--] = tsa[i];
c9f2            rank[sa[1]] = 1;
a5c5            for (int i=2;i<=n;i++){
dc5c                rank[sa[i]] = rank[sa[i-1]];
021c                if (A[sa[i]] != A[sa[i-1]] || B[sa[i]] != B[sa[i-1]])rank[sa[i]]
                        ++;
95cf            }
95cf        }
95cf    }
bbe8    void get_height(int *ch,int n){
0820        get_sa(ch,n);
5c18        sa[0] = rank[0] = 0;
0956        for (int i=1,j=0;i<=n;i++){
1a82            if (j) j--;
757e            while (ch[i+j] == ch[sa[rank[i]-1]+j])j++;
24a7            height[rank[i]] = j;
95cf        }
ed5c#ifdef _DEBUG
6dbf        for (int i=1;i<=n;i++){
dfcf            printf("height[%d]=%d\n",i,height[i]);
95cf        }
1937#endif
4eb6#ifndef RMQ
3b40        segtree.build(1,1,n,height);
a8cb#else
a852        st_init(n,height);
1937#endif
95cf    }
ead2    int get_lcp(int x,int y,int n){
6606        int rkx = rank[x];
a728        int rky = rank[y];
4e5e        if (rkx>rky)swap(rkx,rky);
216a        rkx++;
4eb6#ifndef RMQ
dee6        int lcp = segtree.query(1,1,n,rkx,rky);
a8cb#else
780d        int k = lg[(rky - rkx+1)];
f5b5        int lcp = min(st[rkx][k],st[rky - (1<<k)+1][k]);
1937#endif
427e
ed5c#ifdef _DEBUG
33df        printf("[get_lcp] x=%d y=%d rkx=%d,rky=%d,lcp=%d\n",x,y,rkx,rky,lcp);
1937#endif
        return lcp;                                                          9a6a
    }                                                                        95cf
}sa1,sa2;                                                                    5a1e
int ch2[maxn];                                                               96d9
vector<Run> get_run(int*ch,int n){                                           4d50
    sa1.get_height(ch,n);                                                    7c77
    for (int i=0;i<=n+1;i++){                                                842e
        ch2[i] = ch[i];                                                      13b4
    }                                                                        95cf
    reverse(ch2+1,ch2+1+n);                                                  7db6
    sa2.get_height(ch2,n);                                                   945d
    vector<Run> result(0);                                                   c4b1
    int len_max = n/2;                                                       a2dc
    for (int len = 1;len <=len_max;len ++){                                  dbca
        //get_len_run                                                        427e
        for (int i=1;i<=n;i+=len){                                           870e
            int j = i+len;                                                   d3da
            if (j >n)break;                                                  dd33
            int lcp = sa1.get_lcp(i,j,n);                                    f2a5
            int lcs = sa2.get_lcp(n+1-i,n+1-j,n);                            8ef0
            lcp = min(lcp,len);                                              f20d
            lcs = min(lcs,len);                                              97fa
            assert(j+lcp-1<=n);                                              2cd9
            assert(i-lcs+1>=1);                                              6a34
#ifdef _DEBUG                                                               ed5c
            printf("i=%d,j=%d,len=%d,lcp=%d,lcs=%d\n",i,j,len,lcp,lcs);      8dbc
#endif                                                                      1937
            if (lcp + lcs - 1 < len)continue;                                37d6
            int L = j-lcs+1;                                                 09d8
            int R = j + lcp -1;                                              856e
            result.push_back((Run){L,R,len});                                ab80
        }                                                                    95cf
    }                                                                        95cf
#ifdef _DEBUG                                                               ed5c
    for (Run run : result){                                                  7d48
        printf("[run]: l=%d, r=%d,k=%d\n",run.l,run.r,run.k);                7252
    }                                                                        95cf
#endif                                                                      1937
    return result;                                                           56b0
}                                                                            95cf
int n;                                                                       5c83
typedef long long ll;                                                        4085
ll spanning_forest(vector<Run> &runs){                                       aec3
    sort(runs.begin(),runs.end(),[](Run x,Run y){                            4f70
```

```
b6e2         return w[x.k] < w[y.k];
b251     });
19f3     ll ans = 0;
ec84     for (auto& R : runs) {
de4b         int l = R.l, r = R.r;
bbac         ans += 1ll * merge(l - R.k, l, r - l + 1) * w[R.k];
95cf     }
4206     return ans;
95cf }
7767 int ch[maxn];
3117 int main(){
c592     for (int i=2;i<maxn;i++)lg[i] = lg[i/2] + 1;
9523     int T;
1fd9     scanf("%d",&T);
60ca     while (T--){
cd91         scanf("%d",&n);
4721         for (int i = 0; i < 20 ; i++) ufs[i].init(n);
d15f         ch[n+1] = -1;
d442         ch[0] = -1;
6dbf         for (int i=1;i<=n;i++){
b3d6             scanf("%d",ch+i);
95cf         }
9f8e         int m = n/2;
e052         for (int i=1;i<=m;i++){
ef59             scanf("%d",w+i);
95cf         }
3690         vector<Run> all_run = get_run(ch,n);
1ccd         printf("%lld\n",spanning_forest(all_run));
95cf     }
7021     return 0;
95cf }
```

1.7 Trie Graph

```
427e // Created by calabash_boy on 2019/10/25.
302f #include <bits/stdc++.h>
421c using namespace std;
eb45 const int maxn = 2e5 + 100;
a281 struct Trie {
4562     int nxt[maxn][26], fail[maxn];
427e     // the node I should go when append a character
95ce     int Go[maxn][26];
e7b0     int root = 0;
8abb     int cnt = 0;
1126     void clear(){
082c         root = cnt = 0;
21a1         memset(nxt[0],0,sizeof nxt[0]);
95cf     }
ee91     int newnode() {
6fb3         cnt++;
427e         //clear memory
6808         return cnt;
95cf     }
9bb4     void insert(char *s) {
8f56         int now = root;
f205         while (*s){
3c7d             now = insert(now,*s - 'a');
85be             s ++;
95cf         }
95cf     }
7e27     int insert(int pre, int ch) {
721c         return nxt[pre][ch]?nxt[pre][ch] : nxt[pre][ch] = newnode();
95cf     }
2114     void build() {
aafa         queue<int> Q;
98ae         Q.push(0);
8b79         memcpy(Go[0],nxt[0],sizeof nxt[0]);
11e5         while (!Q.empty()) {
fda7             int head = Q.front();
f2f8             Q.pop();
b3c9             for (int ch = 0; ch < 26; ch++) {
ec9d                 int v = nxt[head][ch];
e151                 if (!v)continue;
eb93                 if (head == 0) fail[v] = 0;
f8d4                 else fail[v] = Go[fail[head]][ch];
2616                 memcpy(Go[v],Go[fail[v]],sizeof Go[v]);
fbe7                 for (int cc = 0; cc < 26; cc++) {
1696                     if (nxt[v][cc])Go[v][cc] = nxt[v][cc];
95cf                 }
78e5                 Q.push(v);
95cf             }
95cf         }
95cf     }
1cc7 }trie;
```

1.8 Trie Graph (Segment Tree)

```
427e // Created by calabash_boy on 2019/10/27.
302f #include <bits/stdc++.h>
421c using namespace std;
eb45 const int maxn = 2e5 + 100;
5c83 int n;
cac6 int p[maxn], c[maxn];
80b8 struct Node{
09de     int lson,rson;
d26b     int val;
5d53     void init(){
c44c         val = 0;
8d91         lson = rson = -1;
95cf     }
37bf }nodes[maxn * 25];
fb8d int node_cnt = 1;
1a67 int build(int x,int l,int r){
d06a     int now = node_cnt ++;
40b6     nodes[now].init();
11a1     if (l == r) return now;
b8b7     int mid = l + r >> 1;
5acf     nodes[now].lson = build(x<<1,l,mid);
aa85     nodes[now].rson = build(x<<1|1,mid+1,r);
7d47     return now;
95cf }
d47b int update(int id,int l,int r,int pos,int val){
d06a     int now = node_cnt ++;
4890     nodes[now] = nodes[id];
3a0d     if (l == r){
1ca8         nodes[now].val = val;
7d47         return now;
95cf     }
b8b7     int mid = l + r >> 1;
7f3f     if (pos <= mid)nodes[now].lson = update(nodes[id].lson,l,mid,pos,val);
f7bd     else nodes[now].rson = update(nodes[id].rson,mid+1,r,pos,val);
7d47     return now;
95cf }
8c6a int query(int id,int l,int r,int pos){
3b8e     if (l == r)return nodes[id].val;
b8b7     int mid = l + r >> 1;
5f37     if (pos <= mid)return query(nodes[id].lson,l,mid,pos);
4f01     else return query(nodes[id].rson,mid+1,r,pos);
95cf }
```

```
a281 struct Trie{
2b0c     map<int,int> nxt[maxn];
3f8e     int root[maxn], fail[maxn];
9991     int cnt = 1;
7e27     int insert(int pre,int ch) {
be19         return nxt[pre].find(ch) == nxt[pre].end() ? nxt[pre][ch] = cnt++ : nxt[
               pre][ch];
95cf     }
2114     void build(){
6eec         queue<int> Q;Q.push(0);
b254         root[0] = ::build(1,1,n);
b72d         for (auto edge : nxt[0]){
8cca             int v,ch;
1822             tie(ch,v) = edge;
81f5             root[0] = update(root[0],1,n,ch,v);
95cf         }
11e5         while (!Q.empty()){
ff8a             int head = Q.front();Q.pop();
567d             for (auto edge: nxt[head]){
8cca                 int v,ch;
1822                 tie(ch,v) = edge;
eb93                 if (head == 0)fail[v] = 0;
f3d0                 else fail[v] = query(root[fail[head]],1,n,ch);
8f45                 root[v] = root[fail[v]];
5943                 for (auto edge2 : nxt[v]){
f96a                     int v2,ch2;
b306                     tie(ch2,v2) = edge2;
4009                     root[v] = update(root[v],1,n,ch2,v2);
95cf                 }
78e5                 Q.push(v);
95cf             }
95cf         }
95cf     }
1cc7 }trie;
3117 int main(){
e1b6     cin>>n;
6dbf     for (int i=1;i<=n;i++){
176e         scanf("%d",p+i);
95cf     }
6dbf     for (int i=1;i<=n;i++){
d09f         scanf("%d",c+i);
1d4a         trie.insert(p[i],c[i]);
95cf     }
c3f5     trie.build();
```

```
6dbf     for (int i=1;i<=n;i++){
7f97         cout<<trie.fail[i] <<"␣";
95cf     }
3251     cout<<endl;
7021     return 0;
95cf }
```

1.9 Dictionary of Basic Factors

```
427e // Created by calabash_boy on 2019/10/28.
427e // CF 100962D 求区间border series，最大border。
b54d #pragma GCC optimize(3)
302f #include <bits/stdc++.h>
18f5 #define rank rkrkrk
421c using namespace std;
96ad const int maxn = 4e5 + 100;
8b50 const int maxlog = 19;
5690 struct Sequence{
bd2b     /** l + k*d <=r **/
6bee     int l,r,d;
f41b     Sequence(int ll = 0,int rr = 0,int dd = 0){
9e51         l = ll;r = rr;d = dd;
95cf     }
3e46     Sequence(const vector<int> & pos){
83e6         if (pos.empty()){
7629             l = r = d = 0;
5620         }else if (pos.size() == 1){
651d             l = pos.front();
8790             r = pos.front();
4753             d = 1;
8e2e         }else{
651d             l = pos.front();
603d             r = pos.back();
7cad             d = pos[1] - pos[0];
95cf         }
95cf     }
b065     bool has(int x){
5ca2         return d and x >= l and x <= r and x % d == l % d;
95cf     }
5bcc     int count(){
c7de         if (d == 0)return 0;
9916         return (r - l) / d + 1;
95cf     }
4083     vector<int> to_list(){
dc6c         vector<int> list(0);
02b2         if (d == 0)return list;
7a3e         for (int i=l;i<=r;i+=d)list.push_back(i);
7b4d         return list;
95cf     }
329b };
a950 Sequence operator -(int X, Sequence S){return Sequence(X - S.r,X - S.l, S.d);}
3997 Sequence operator -(Sequence S, int X){return Sequence(S.l - X, S.r - X, S.d);}
4ad6 Sequence operator &(Sequence S1, Sequence S2){
55d2     int cnt1 = S1.count(), cnt2 = S2.count();
8ea9     if (cnt1 == 0 || cnt2 == 0) return Sequence(0,0,0);
433a     if (cnt1 > cnt2){
8b8f         swap(S1,S2);swap(cnt1,cnt2);
95cf     }
06db     if (cnt1 < 3){
8e82         vector<int> pos(0);
fd94         for (int x : S1.to_list()){
9391             if (S2.has(x)) pos.push_back(x);
95cf         }
94cb         return Sequence(pos);
8e2e     }else{
912e         if (S1.d == S2.d){
2db6             int l = max(S1.l,S2.l), r = min(S1.r,S2.r);
2346             if (r >= l && S1.l % S1.d == S2.l % S1.d)return Sequence(l,r,S1.d);
bf46             else return Sequence(0,0,0);
ddc2         }else assert(0);
95cf     }
95cf }
2f33 struct Run{
427e     //S[l,r] is a run of period of length d.
6bee     int l,r,d;
fc18     Run(int ll = 0,int rr = 0,int dd = 0){
9e51         l = ll;r = rr;d = dd;
95cf     }
04f0     bool operator < (const Run &other)const{
fc87         if (l != other.l)return l < other.l;
7836         if (r != other.r)return r < other.r;
a241         if (d != other.d)return d < other.d;
438e         return false;
95cf     }
b8bc     bool operator == (const Run &other)const{
98a4         return l == other.l and r == other.r and d == other.d;
```

```
95cf     }
329b };
dcc9 struct Dictionary_of_Basic_Factories{
6ebf     /** 1-base **/
4d80     int name[maxn][maxlog];int n;
64b3     vector<vector<int> > pos[maxlog];
6e4f     int cntA[maxn],cntB[maxn],tsa[maxn],A[maxn],B[maxn];
a540     int sa[maxn],rank[maxn];
c3e5     int height[maxn];
1126     void clear(){
26c3         for (int i=0;i<=max(n,'z' + 10);i++){
0808             cntA[i] = cntB[i] = tsa[i] = A[i] = B[i] = sa[i] = rank[i] = height[
                   i] = 0;
d71d             for (int k=0;k<maxlog;k++)name[i][k] = 0;
95cf         }
67d7         for (int k=0;k<maxlog;k++)pos[k].clear();
95cf     }
8ea9     void init(char * ch,int n){
316e         ch[0] = ch[n+1] = '#'; this->n = n;
e86b         for (int i=1;i<=n;i++)cntA[ch[i]]++;
a49f         for (int i=1;i<maxn;i++)cntA[i] += cntA[i-1];
625e         for (int i=n;i>=1;i--)sa[cntA[ch[i]]--] = i;
c9f2         rank[sa[1]] = 1;
a5c5         for (int i=2;i<=n;i++){
dc5c             rank[sa[i]] = rank[sa[i-1]];
459c             if (ch[sa[i]] != ch[sa[i-1]])rank[sa[i]] ++;
95cf         }
b7da         pos[0].resize(rank[sa[n]] + 1,vector<int>(0));
6dbf         for (int i=1;i<=n;i++){
fa1a             name[i][0] = rank[i];
b708             pos[0][rank[i]].push_back(i);
95cf         }
a867         for (int step = 1,l=1;l <= n;l<<=1,step ++){
c794             for (int i=0;i<=n;i++)cntA[i] = cntB[i] = 0;
6dbf             for (int i=1;i<=n;i++){
d9ab                 cntA[A[i] = rank[i]] ++;
c846                 cntB[B[i]=(i+l<=n)?rank[i+l]:0]++;
95cf             }
72d7             for (int i=1;i<=n;i++)cntB[i] += cntB[i-1];
4c62             for (int i=n;i>=1;i--)tsa[cntB[B[i]]--] = i;
c35a             for (int i=1;i<=n;i++)cntA[i] += cntA[i-1];
1626             for (int i=n;i>=1;i--)sa[cntA[A[tsa[i]]]--] = tsa[i];
c9f2             rank[sa[1]] = 1;
a5c5             for (int i=2;i<=n;i++){
dc5c                 rank[sa[i]] = rank[sa[i-1]];
021c                 if (A[sa[i]] != A[sa[i-1]] || B[sa[i]] != B[sa[i-1]])rank[sa[i]]
                       ++;
95cf             }
4d1e             pos[step].resize(rank[sa[n]] + 1,vector<int> (0));
6dbf             for (int i = 1;i <=n;i++){
c0e3                 name[i][step] = rank[i];
5a42                 pos[step][rank[i]].push_back(i);
95cf             }
95cf         }
95cf     }
a8cb void get_height(char *ch, int n){
427e
5c18     sa[0] = rank[0] = 0;
0956     for (int i=1,j=0;i<=n;i++){
1a82         if (j)j--;
757e         while (ch[i+j] == ch[sa[rank[i]-1] +j])j++;
24a7         height[rank[i]]= j;
95cf     }
95cf }
427e // get sequence [2^step,2^(step+1))
7757 Sequence get_seq(vector<int> & list, int l, int r){
8e82     vector<int> pos(0);
5dee     int idx = lower_bound(list.begin(),list.end(),l) - list.begin();
6a21     while (idx < list.size() && pos.size() < 3 && list[idx] <= r){
7d69         pos.push_back(list[idx]);idx ++;
95cf     }
8d9e     if (pos.size() < 3)return Sequence(pos);
037f     else{
b0ae         int last = upper_bound(list.begin(),list.end(),r) - list.begin() -
               1;
88c2         int L = pos.front(), d = pos[1] - pos[0], R = list[last];
7985         return Sequence(L,R,d);
95cf     }
95cf }
25d0 Sequence get_border(int l,int r,int step){
937e     int len = r - l + 1;
701e     int baby = 1 << step, giant = min(len-1,(baby * 2-1));
ed64     int namel = name[l][step], namer = name[r - baby + 1][step];
681e     Sequence seql = get_seq(pos[step][namel],r - giant + 1,r - baby + 1),
987b             seqr = get_seq(pos[step][namer],l,l + giant - baby);
4d27     seql = (r + 1) - seql; seqr = seqr - (l -baby);
8804     return  seql & seqr;
95cf }
```

```
650b    /** return O(logn) border series of S[l,r].
8265     * Attention: can contain empty sequence (0,0,0)
93ed     * if [2^i,2^(i+1)) border does not exist.*/
83a4    vector<Sequence> get_border_series(int l,int r){
7ae3        vector<Sequence> ret(0);
b085        for (int step = 0;(1<<step) < r - l + 1;step++){
e0c4            ret.push_back(get_border(l,r,step));
95cf        }
ee0f        return ret;
95cf    }
d1cf    int get_biggest_border(int l,int r){
937e        int len = r - l + 1;
121c        for (int k = maxlog - 1; k >=0;k--){
6384            if ((1<<k) >= len)continue;
bb4d            Sequence seq = get_border(l,r,k);
4bab            if (seq.r)return seq.r;
95cf        }
7021        return 0;
95cf    }
4085    int lcp(int x,int y){
babf        int len = 0;
121c        for (int k = maxlog-1;k>=0;k--){
d4df            int LEN = 1<< k;
3727            if (x + LEN - 1 <= n and y + LEN - 1 <= n and name[x][k] == name[y][
                    k]){
4241                len += 1<<k;
ab49                x += 1<<k;
aebb                y += 1<<k;
95cf            }
95cf        }
1891        return len;
95cf    }
7809    int lcs(int x,int y){
babf        int len = 0;
121c        for (int k = maxlog-1;k>=0;k--){
d4df            int LEN = 1 << k;
5b52            if (x >= LEN and y >= LEN and name[x - LEN + 1][k] == name[y - LEN +
                    1][k]){
567e                len += LEN;
4544                x -= LEN;
779f                y -= LEN;
95cf            }
95cf        }
1891        return len;
95cf    }
3731    vector<Run> get_all_runs(){
427e        // cerr<<n<<endl;
0fc8        vector<Run> run_list(0);
1402        for (int per = 1; per * 2 <= n; per ++){
44b8            for (int pos = per;pos <= n;pos += per){
3506                int left = lcs(pos,pos + per);
9a63                int right = lcp(pos,pos + per);
c681                if (left + right > per){
1f79                    run_list.push_back(Run(pos - left + 1,pos + per + right - 1,
                            per));
95cf                }
95cf            }
95cf        }
c4b1        vector<Run> result(0);
d7e0        pair<int,int> pre = {-1,-1};
6dba        for (auto run : run_list){
48fb            pair<int,int> now = {run.l,run.r};
e449            if (pre != now){
f764                pre = now;
0ab8                result.push_back(run);
95cf            }
95cf        }
56b0        return result;
95cf    }
ff99}dbf;
15df char s[maxn];
1ed7 int n,q;
3117 int main(){
5397    scanf("%d%d",&n,&q);
a275    scanf("%s",s + 1);
ac6e    dbf.init(s,n);
2cc8    while (q--){
9f6b        int l,r;
f4d0        scanf("%d%d",&l,&r);
2e80        printf("%d\n",dbf.get_biggest_border(l,r));
95cf    }
7021    return 0;
95cf }
```

2 String Automaton

2.1 ACAM

```
427e // Created by calabash_boy on 18-6-5.
427e // HDU 6138
427e //给定若干字典串。
427e // query:strx stry 求最长的p,p为strx、stry子串，且p为某字典串的前缀
302f #include<bits/stdc++.h>
421c using namespace std;
52c1 const int maxn = 1e5+100;
6b3e struct Aho_Corasick_Automaton{
427e     //basic
141b     int nxt[maxn*10][26],fail[maxn*10];
7a04     int root,tot;
427e     //special
8f42     int flag[maxn*10];
d3a5     int len[maxn*10];
1126     void clear(){
21a1         memset(nxt[0],0,sizeof nxt[0]);
0ae1         root = tot=0;
95cf     }
ee91     int newnode(){
71cf         tot++;
87f4         memset(nxt[tot],0,sizeof nxt[tot]);
a231         flag[tot] = len[tot]=0;
91fb         return tot;
95cf     }
9bb4     void insert(char *s ){
8f56         int now = root;
f205         while (*s){
e37a             int id = *s-'a';
ce8f             if(!nxt[now][id])nxt[now][id] = newnode();
7134             len[nxt[now][id]] = len[now]+1;
6f00             now = nxt[now][id];
95cf         }
95cf     }
bcf9     void insert(string str){
8f56         int now = root;
10ad         for (int i=0;i<str.size();i++){
25da             int id = str[i]-'a';
ce8f             if(!nxt[now][id])nxt[now][id] = newnode();
7134             len[nxt[now][id]] = len[now]+1;
6f00             now = nxt[now][id];
95cf         }
95cf     }
2114     void build(){
30ee         fail[root] = root;
c19d         queue<int>Q;Q.push(root);
11e5         while (!Q.empty()){
ff8a             int head = Q.front();Q.pop();
414f             for (int i=0;i<26;i++){
c591                 if(!nxt[head][i])continue;
762f                 int temp = nxt[head][i];
c509                 fail[temp] = fail[head];
a7fb                 while (fail[temp]&&!nxt[fail[temp]][i]){
5e80                     fail[temp] = fail[fail[temp]];
95cf                 }
3198                 if(head&&nxt[fail[temp]][i])fail[temp] = nxt[fail[temp]][i];
6b09                 Q.push(temp);
95cf             }
95cf         }
95cf     }
fddd     void search(string str,int QID);
cf07     int query(string str,int QID);
5ede }acam;
1874 void Aho_Corasick_Automaton::search(string str,int QID) {
8f56     int now = root;
10ad     for (int i=0;i<str.size();i++){
25da         int id = str[i]-'a';
b2b6         now = nxt[now][id];int temp = now;
694e         while (temp!=root&&flag[temp]!=QID){
22a4             flag[temp] = QID;
f597             temp = fail[temp];
95cf         }
95cf     }
95cf }
126b int Aho_Corasick_Automaton::query(string str, int QID) {
81f4     int ans =0;int now = root;
10ad     for (int i=0;i<str.size();i++){
25da         int id = str[i]-'a';
6f00         now = nxt[now][id];
c20a         int temp = now;
dead         while (temp!=root){
497d             if(flag[temp]==QID){
79cd                 ans = max(ans,len[temp]);
6173                 break;
```

```
95cf            }
f597            temp = fail[temp];
95cf        }
95cf    }
4206    return ans;
95cf}
fae2string a[maxn];
24dfint m,n,qid;
3117int main(){
42db    int T;cin>>T;
60ca    while (T--){
67f3        acam.clear();cin>>n;
6dbf        for (int i=1;i<=n;i++){
879c            cin>>a[i];
e321            acam.insert(a[i]);
95cf        }
1ccd        acam.build();cin>>m;
e052        for (int i=1;i<=m;i++){
74ca            int x,y;cin>>x>>y;
6a4f            qid++;
071c            acam.search(a[x],qid);
c2f3            int ans = acam.query(a[y],qid);
d592            cout<<ans<<endl;
95cf        }
95cf    }
7021    return 0;
95cf}
```

2.2 SAM

```
427e// Created by calabash_boy on 18-6-4.
427e//SPOJ substring
427e// calc ans_i=长度=i的所有子串，出现次数最多的一种出现了多少次。
302f#include<bits/stdc++.h>
374e#define RIGHT
427e//RIGHT: parent树的dfs序上主席树，求每个点的Right集合
421cusing namespace std;
40fbconst int maxn = 25e4+100;
dd0f#ifdef RIGHT
d273struct Node{int L,R,val;}Tree[maxn*40];
6207struct Chairman_Tree{
8abb    int cnt = 0;
bd4f    int root[maxn*2];
5d53    void init(){
a4f5        memset(root,0,sizeof root);
8766        cnt =0;
95cf    }
94cf    /* 建T0空树 */
cf84    int buildT0(int l, int r){
64f2        int k = cnt++;
ecaf        Tree[k].val =0;
eb40        if (l==r) return k;
b8b7        int mid = l+r >>1;
0bf4        Tree[k].L = buildT0(l, mid);Tree[k].R = buildT0(mid + 1, r);
e27b        return k;
95cf    }
e965    /* 上一个版本节点P，【ppos】+=del 返回新版本节点*/
3a6b    int update (int P,int l,int r,int ppos,int del){
d4b1        assert(cnt < maxn*50);
64f2        int k = cnt++;
73d2        Tree[k].val = Tree[P].val +del;
eb40        if (l==r) return k;
b8b7        int mid = l+r >>1;
4af7        if (ppos<=mid){
5b36            Tree[k].L = update(Tree[P].L,l,mid,ppos,del);
de01            Tree[k].R = Tree[P].R;
8e2e        }else{
0d44            Tree[k].L = Tree[P].L;
a179            Tree[k].R = update(Tree[P].R,mid+1,r,ppos,del);
95cf        }
e27b        return k;
95cf    }
b13a    int query(int PL,int PR,int l,int r,int L,int R){
b8e7        if (l>R || L>r)return 0;
03d9        if (L <= l && r <= R)return Tree[PR].val - Tree[PL].val;
b8b7        int mid = l + r >> 1;
ff4f        return query(Tree[PL].L,Tree[PR].L,l,mid,L,R) + query(Tree[PL].R,Tree[PR
              ].R,mid+1,r,L,R);
95cf    }
b0c1}tree;
1937#endif
6f83char s[maxn];int n,ans[maxn];
8a63/*注意需要按l将节点基数排序来拓扑更新parent树*/
3e3estruct Suffix_Automaton{
427e    //basic
0037    int nxt[maxn*2][26],fa[maxn*2],l[maxn*2];
```

```
0db0     int last,cnt;
427e     //extension
f6ac     int cntA[maxn*2],A[maxn*2];/*辅助拓扑更新*/
b0fc     int num[maxn*2];/*每个节点代表的所有串的出现次数*/
dd0f #ifdef RIGHT
0641     vector<int> E[maxn*2];
6561     int dfsl[maxn*2],dfsr[maxn*2],dfn;
4296     int pos[maxn*2];
efe5     int end_pos[maxn*2];//1基
1937 #endif
c75a     Suffix_Automaton(){ clear(); }
1126     void clear(){
651a         last =cnt=1;
63e2         fa[1]=l[1]=0;
9b85         memset(nxt[1],0,sizeof nxt[1]);
95cf     }
e798     void init(char *s){
f205         while (*s){
d3f9             add(*s-'a');s++;
95cf         }
95cf     }
681b     void add(int c){
a4cf         int p = last;
4428         int np = ++cnt;
8b9f         memset(nxt[cnt],0,sizeof nxt[cnt]);
97c0         l[np] = l[p]+1;last = np;
b7f5         while (p&&!nxt[p][c])nxt[p][c] = np,p = fa[p];
fdc4         if (!p)fa[np]=1;
037f         else{
5740             int q = nxt[p][c];
d84d             if (l[q]==l[p]+1)fa[np] =q;
037f             else{
2401                 int nq = ++ cnt;
bc67                 l[nq] = l[p]+1;
da26                 memcpy(nxt[nq],nxt[q],sizeof (nxt[q]));
66a6                 fa[nq] =fa[q];fa[np] = fa[q] =nq;
5dc1                 while (nxt[p][c]==q)nxt[p][c] =nq,p = fa[p];
95cf             }
95cf         }
95cf     }
2114     void build(){
4006         memset(cntA,0,sizeof cntA);
7b40         memset(num,0,sizeof num);
1a84         for (int i=1;i<=cnt;i++)cntA[l[i]]++;
856c         for (int i=1;i<=cnt;i++)cntA[i]+=cntA[i-1];
ebb3         for (int i=cnt;i>=1;i--)A[cntA[l[i]]--] =i;
f42d         /*更行主串节点*/
3c9b         int temp=1;
1294         for (int i=0;i<n;i++){
3bd2             num[temp = nxt[temp][s[i]-'a'] ]=1;
95cf         }
e1a0         /*拓扑更新*/
5258         for (int i=cnt;i>=1;i--){
427e             //basic
b7fa             int x = A[i];
32d6             num[fa[x]]+=num[x];
427e             //special
f982             ans[l[x]] = max(ans[l[x]],num[x]);
95cf         }
427e         //special
66f2         for (int i=l[last];i>1;i--){
88a3             ans[i-1] = max(ans[i-1],ans[i]);
95cf         }
95cf     }
427e
dd0f #ifdef RIGHT
a1e1     int get_right_between(int u,int l,int r){
64ba         return tree.query(tree.root[dfsl[u] - 1],tree.root[dfsr[u]],1,::n,l,r);
95cf     }
d714     void dfs(int u){
2b56         dfsl[u] = ++ dfn;
98d9         pos[dfn] = u;
2c0f         for (int v : E[u]){
5f3c             dfs(v);
95cf         }
64a8         dfsr[u] = dfn;
95cf     }
0350     void extract_right(){
3c9b         int temp = 1;
1294         for (int i=0;i<n;i++){
ac16             temp = nxt[temp][s[i] - 'a'];
6940             end_pos[temp] = i+1;
95cf         }
f6b7         for (int i=2;i<=cnt;i++){
5e80             E[fa[i]].push_back(i);
95cf         }
0426         dfn = 0;
dcdd         dfs(1);
```

```
5087        tree.root[0] = tree.buildT0(1,n);
7b35        for (int i=1;i<=cnt;i++){
cda5            int u = pos[i];
1c34            if (end_pos[u]){
9965                int idx = end_pos[u];
b360                tree.root[i] = tree.update(tree.root[i-1],1,n,idx,1);
8e2e            }else{
d757                tree.root[i] = tree.root[i-1];
95cf            }
95cf        }
95cf    }
1937 #endif
56dd    void debug(){
5258        for (int i=cnt;i>=1;i--){
01ab            printf("num[%d]=%d l[%d]=%d fa[%d]=%d\n",i,num[i],i,l[i],i,fa[i]);
95cf        }
95cf    }
5eed }sam;
3117 int main(){
587c    scanf("%s",s);
aaa0    /* calc n must before sam.init()*/
5264    n = strlen(s);
84b5    sam.init(s);
bb59    sam.build();
6dbf    for (int i=1;i<=n;i++){
6240        printf("%d\n",ans[i]);
95cf    }
7021    return 0;
95cf }
```

2.3 Generlized SAM

```
427e // Created by calabash_boy on 19-4-5.
427e //wf2019 first of her name
427e //build sam using trie
302f #include<bits/stdc++.h>
421c using namespace std;
94a1 const int maxn = 1e6+100;
4085 typedef long long ll;
3e3e struct Suffix_Automaton{
0037    int nxt[maxn*2][26],fa[maxn*2],l[maxn*2];
0db0    int last,cnt;
0641    vector<int> E[maxn*2];
61cb    int Num[maxn*2];
c75a    Suffix_Automaton(){ clear(); }
1126    void clear(){
651a        last =cnt=1;
63e2        fa[1]=l[1]=0;
9b85        memset(nxt[1],0,sizeof nxt[1]);
95cf    }
6cab    int add(int pre,int c,int num){
2d24        last = pre;
a4cf        int p = last;
4428        int np = ++cnt;
b844        Num[np] = num;
8b9f        memset(nxt[cnt],0,sizeof nxt[cnt]);
97c0        l[np] = l[p]+1;last = np;
b7f5        while (p&&!nxt[p][c])nxt[p][c] = np,p = fa[p];
fdc4        if (!p)fa[np]=1;
037f        else{
5740            int q = nxt[p][c];
d84d            if (l[q]==l[p]+1)fa[np] =q;
037f            else{
2401                int nq = ++ cnt;
bc67                l[nq] = l[p]+1;
da26                memcpy(nxt[nq],nxt[q],sizeof (nxt[q]));
66a6                fa[nq] =fa[q];fa[np] = fa[q] =nq;
5dc1                while (nxt[p][c]==q)nxt[p][c] =nq,p = fa[p];
95cf            }
95cf        }
597e        return np;
95cf    }
b432    int dfsl[maxn*2],dfsr[maxn*2];
b4c2    int dfn = 0;
45bd    ll sum[maxn*2];
d714    void dfs(int u){
2b56        dfsl[u] = ++dfn;
445a        sum[dfn] = Num[u];
2c0f        for (int v : E[u]){
5f3c            dfs(v);
95cf        }
64a8        dfsr[u] = dfn;
95cf    }
2114    void build(){
f6b7        for (int i=2;i<=cnt;i++){
5e80            E[fa[i]].push_back(i);
```

```
95cf        }
dcdd        dfs(1);
7b35        for (int i=1;i<=cnt;i++){
036a            sum[i] += sum[i-1];
95cf        }
95cf    }
c250    void query(char * s){
3c9b        int temp = 1;
f205        while (*s){
6147            int ch = *s - 'A';
323f            if (!nxt[temp][ch]){
3257                printf("0\n");
4f2d                return;
95cf            }
9439            temp = nxt[temp][ch];
85be            s++;
95cf        }
a64e        ll ans = sum[dfsr[temp]] - sum[dfsl[temp] - 1];
8542        printf("%lld\n",ans);
95cf    }
5eed }sam;
a281 struct Trie{
f142    int Root = 1;
e317    int cnt = 2;
e2e6    int nxt[maxn][26];
dd2d    int num[maxn];
75bc    int sam_pos[maxn];
1f95    int add(int p,int ch){
2e0c        if (!nxt[p][ch]){
621d            nxt[p][ch] = cnt++;
95cf        }
86e9        int now = nxt[p][ch];
e204        num[now] ++;
7d47        return now;
95cf    }
06b4    void bfs(){
aafa        queue<int> Q;
4ad5        Q.push(1);
4f25        sam_pos[1] = 1;
11e5        while (!Q.empty()){
fda7            int head = Q.front();
f2f8            Q.pop();
414f            for (int i=0;i<26;i++){
c591                if (!nxt[head][i])continue;
2f97                int now = nxt[head][i];
7ee9                sam_pos[now] = sam.add(sam_pos[head],i,num[now]);
e77a                Q.push(now);
95cf            }
95cf        }
95cf    }
1cc7 }trie;
2616 int trie_pos[maxn];
3117 int main(){
232a    int n,k;
9927    scanf("%d%d",&n,&k);
7b34    trie_pos[0] = 1;
6dbf    for (int i=1;i<=n;i++){
66c9        static char s[5];
4ec4        int p;
66ef        scanf("%s%d",s,&p);
d259        int ch = s[0] - 'A';
faf2        trie_pos[i] = trie.add(trie_pos[p],ch);
95cf    }
49c4    trie.bfs();
bb59    sam.build();
f3ea    for (int i=0;i<k;i++){
8fa9        static char t[maxn];
f184        scanf("%s",t);
56bc        int N = strlen(t);
7bd6        reverse(t,t+N);
3c43        sam.query(t);
95cf    }
7021    return 0;
95cf }
```

2.4 C-SAM(CDAWG)

```
427e // Created by calabash_boy on 2019/11/5.
427e // 求后缀树的每条边代表字符串的本质不同子串个数的和
427e // 后缀树边上字符串unique之后总长度为3*n.
427e // unique的结果与压缩sam上的边相同。
302f #include <bits/stdc++.h>
421c using namespace std;
6f64 const int maxn = 5e5 + 100;
4085 typedef long long ll;
3e3e struct Suffix_Automaton{
```

```
0037    int nxt[maxn*2][26],fa[maxn*2],l[maxn*2];
e21c    bool vis[maxn*2];
1ca4    int dirNxt[maxn*2][26];
ceb8    int dirLen[maxn*2][26];
6070    int ed[maxn*2];
65a0    vector<pair<int,int> > lens[maxn*2];
0db0    int last,cnt;
1126    void clear(){
651a        last =cnt=1;
63e2        fa[1]=l[1]=0;
9b85        memset(nxt[1],0,sizeof nxt[1]);
95cf    }
33b9    void init(string s){
90a8        for (int c : s)add(c - 'a');
0fc1        for (int i=0;i<=cnt;i++){
0cd8            vis[i] = false;
9673            ed[i] = -1;
d6a5            lens[i].clear();
8f42            memset(dirLen[i],0,sizeof dirLen[i]);
da3a            memset(dirNxt[i],0,sizeof dirNxt[i]);
95cf        }
95cf    }
681b    void add(int c){
a4cf        int p = last;
4428        int np = ++cnt;
8b9f        memset(nxt[cnt],0,sizeof nxt[cnt]);
97c0        l[np] = l[p]+1;last = np;
b7f5        while (p&&!nxt[p][c])nxt[p][c] = np,p = fa[p];
fdc4        if (!p)fa[np]=1;
037f        else{
5740            int q = nxt[p][c];
d84d            if (l[q]==l[p]+1)fa[np] =q;
037f            else{
2401                int nq = ++ cnt;
bc67                l[nq] = l[p]+1;
da26                memcpy(nxt[nq],nxt[q],sizeof (nxt[q]));
66a6                fa[nq] =fa[q];fa[np] = fa[q] =nq;
5dc1                while (nxt[p][c]==q)nxt[p][c] =nq,p = fa[p];
95cf            }
95cf        }
95cf    }
5a6f    int find_nxt(int u){
868a        int res = -1;
b3c9        for (int ch = 0;ch < 26;ch ++){
ea10            int v = nxt[u][ch];
e151            if (!v)continue;
ee4b            if (res == -1)res = ch;
4796            else return -1;
95cf        }
244d        return res;
95cf    }
d714    void dfs(int u){
6cfd        vis[u] = true;
b3c9        for (int ch = 0;ch < 26;ch ++){
ea10            int v = nxt[u][ch];
e151            if (!v)continue;
384d            if (!vis[v])dfs(v);
c21d            int dirch = find_nxt(v);
4ff2            if(dirch == -1){
31a6                dirNxt[u][ch] = v;
b309                dirLen[u][ch] = 1;
8e2e            }else{
1896                dirNxt[u][ch] = dirNxt[v][dirch];
bc25                dirLen[u][ch] = dirLen[v][dirch] + 1;
95cf            }
a3aa            if (find_nxt(u) == -1 or u == 1)lens[dirNxt[u][ch]].push_back(
                  make_pair(dirLen[u][ch],u == 1?1:l[u] - l[fa[u]]));
329b        };
95cf    }
5c37    void build(string s,Suffix_Automaton & sam_t){
3c9b        int temp = 1;
6545        for(int i=0;i<s.length();i++){
ac16            temp = nxt[temp][s[i] - 'a'];
33af            int t = temp;
294a            while (ed[t] == -1 && t != 1){
b78e                ed[t] = i;
44bb                t = fa[t];
95cf            }
95cf        }
19f3        ll ans = 0;
f6b7        for (int i=2;i<=cnt;i++){
e538            if (lens[i].empty())continue;
a8af            int Mx = 0;
df85            for (auto x : lens[i])Mx = max(Mx,x.first);
0bb1            string t = s.substr(ed[i] - Mx + 1,Mx);
8f31            sam_t.clear();
fa94            reverse(t.begin(),t.end());
9fa9            vector<ll> cnt(1,0);
```

```
            for (int c : t){
                sam_t.add(c - 'a');
                cnt.push_back(cnt.back() + sam_t.l[sam_t.last] - sam_t.l[sam_t.
                  fa[sam_t.last]]);
            }
            for (auto x : lens[i])ans += cnt[x.first] * x.second;
        }
        cout<<ans<<endl;
    }
}sam,temp_sam;
int main(){
    int T;
    cin>>T;
    while (T--){
        string s;
        cin>>s;
        sam.clear();
        sam.init(s);
        sam.dfs(1);
        sam.build(s,temp_sam);
    }
    return 0;
}
```

2.5 PAM

```
// Created by calabash_boy on 18-6-4.
// BZOJ 3676
// calc max(len(t)*cnt(t)) t为s回文子串，cnt(t)=t出现次数
#include<bits/stdc++.h>
using namespace std;
const int maxn = 3e5+100;
struct Palindromic_AutoMaton{
    //basic
    int s[maxn],now;
    int nxt[maxn][26],fail[maxn],l[maxn],last,tot;
    // extension
    int num[maxn];/*节点代表的所有回文串出现次数*/
    void clear(){
        //1节点：奇数长度root 0节点：偶数长度root
        s[0]=l[1]=-1;
        fail[0] = tot = now =1;
        last = l[0]=0;
        memset(nxt[0],0,sizeof nxt[0]);
        memset(nxt[1],0,sizeof nxt[1]);
    }
    Palindromic_AutoMaton(){clear();}
    int newnode(int ll){
        tot++;
        memset(nxt[tot],0,sizeof nxt[tot]);
        fail[tot]=num[tot]=0;
        l[tot]=ll;
        return tot;
    }
    int get_fail(int x){
        while (s[now-l[x]-2]!=s[now-1])x = fail[x];
        return x;
    }
    void add(int ch){
        s[now++] = ch;
        int cur = get_fail(last);
        if(!nxt[cur][ch]){
            int tt = newnode(l[cur]+2);
            fail[tt] = nxt[get_fail(fail[cur])][ch];
            nxt[cur][ch] = tt;
        }
        last = nxt[cur][ch];num[last]++;
    }
    void build(){
        //fail[i]<i，拓扑更新可以单调扫描。
        for (int i=tot;i>=2;i--){
            num[fail[i]]+=num[i];
        }
        num[0]=num[1]=0;
    }
    void init(char* ss){
        while (*ss){
            add(*ss-'a');ss++;
        }
    }
    void init(string str){
        for (int i=0;i<str.size();i++){
            add(str[i]-'a');
        }
    }
    long long query();
```

```
}pam;
long long Palindromic_AutoMaton::query(){
    long long ret =1;
    for (int i=2;i<=tot;i++){
        ret = max(ret,1LL*l[i]*num[i]);
    }
    return ret;
}
char s[maxn];
int main(){
    scanf("%s",s);
    pam.init(s);
    pam.build();
    printf("%lld\n",pam.query());
    return 0;
}
```

2.6 区间本质不同子串

```
/* Created by calabash_boy on 19-12-4.
 * tutorial:
 *https://codeforces.com/blog/entry/62331?tdsourcetag=s_pctim_aiomsg
 */
#include<bits/stdc++.h>
using namespace std;
typedef long long ll;
const int maxn = 1e5 + 100;
/* 维护最后出现位置在i（左端点）的本质不同串数量 */
struct SegmentTree_Sum{
    ll Sum[maxn * 8],Lazy[maxn*8];
    void down(int x,int l,int mid,int r){
        Sum[x<<1] += Lazy[x] * (mid - l + 1);
        Sum[x<<1|1] += Lazy[x] * (r - mid);
        Lazy[x<<1] += Lazy[x];
        Lazy[x<<1|1] += Lazy[x];
        Lazy[x] = 0;
    }
    void up(int x){Sum[x] = Sum[x<<1] + Sum[x<<1|1];}
    void update(int x,int l,int r,int L,int R,int val){
        if (l > R or L > r)return;
        if (L <= l and r <= R){
            Sum[x] += 1ll * val * (r - l + 1);
            Lazy[x] += val;
            return;
        }
        int mid = l + r >> 1;down(x,l,mid,r);
        update(x<<1,l,mid,L,R,val);update(x<<1|1,mid+1,r,L,R,val);
        up(x);
    }
    ll query(int x,int l,int r,int L,int R){
        if (l > R or L > r)return 0;
        if (L <= l and r <= R)return Sum[x];
        int mid = l + r >> 1;down(x,l,mid,r);
        return query(x<<1,l,mid,L,R) + query(x<<1|1,mid+1,r,L,R);
    }
}segtree;
struct SegmentTree_Max{
    int Max[maxn*8];
    void update(int x,int l,int r,int pos,int val){
        Max[x] = max(Max[x],val);
        if (l == r)return;
        int mid = l + r >> 1;
        if (pos <= mid)update(x<<1,l,mid,pos,val);
        else update(x<<1|1,mid+1,r,pos,val);
    }
    int query(int x,int l,int r,int L,int R){
        if (l > R or L > r)return -1;
        if (L <= l and r <= R)return Max[x];
        int mid = l + r >> 1;
        return max(query(x<<1,l,mid,L,R),query(x<<1|1,mid+1,r,L,R));
    }
}dfstree;
int n,q;
char s[maxn];
ll ans[maxn];
typedef pair<pair<int,int>,int> Query;
vector<Query> query;
struct Suffix_Automaton{
    int nxt[maxn*2][26],fa[maxn*2],l[maxn*2];
    int last,cnt;
    /* 每个color最上边一个点 */
    int up_to[maxn];
    /* 是否被染过色 */
    bool used[maxn*2];
    Suffix_Automaton(){ clear(); }
    void clear(){
```

```
8bdb        last =cnt=1;fa[1]=l[1]=0;
9b85        memset(nxt[1],0,sizeof nxt[1]);
95cf    }
e798    void init(char *s){
0bef        while (*s){add(*s-'a');s++;}
95cf    }
681b    void add(int c){
a4cf        int p = last;
4428        int np = ++cnt;
8b9f        memset(nxt[cnt],0,sizeof nxt[cnt]);
97c0        l[np] = l[p]+1;last = np;
b7f5        while (p&&!nxt[p][c])nxt[p][c] = np,p = fa[p];
fdc4        if (!p)fa[np]=1;
037f        else{
5740            int q = nxt[p][c];
d84d            if (l[q]==l[p]+1)fa[np] =q;
037f            else{
2401                int nq = ++ cnt;
bc67                l[nq] = l[p]+1;
da26                memcpy(nxt[nq],nxt[q],sizeof (nxt[q]));
66a6                fa[nq] =fa[q];fa[np] = fa[q] =nq;
5dc1                while (nxt[p][c]==q)nxt[p][c] =nq,p = fa[p];
95cf            }
95cf        }
95cf    }
0641    vector<int> E[maxn * 2];
14d9    int in[maxn*2],out[maxn*2],dfn;
d714    void dfs(int u){
c964        in[u] = ++dfn;
905c        for (int v:E[u])dfs(v);
5383        out[u] = dfn;
95cf    }
eb55    void gao(){
e3bd        for (int i=2;i<=cnt;i++)E[fa[i]].push_back(i);
dcdd        dfs(1);
922c        for (int i=1,now = 1;i<=n;i++){
fc61            now = nxt[now][s[i] - 'a'];
de8e            assert(l[now] == i);
c927            segtree.update(1,1,n,1,i,1);
228a            int u = now;
9ad1            while (u != 1 and !used[u]){
191b                used[u] = true;
dd8a                u = fa[u];
95cf            }
```

```
9b7c            while (u != 1){
9ccc                int cur = dfstree.query(1,1,cnt,in[u],out[u]);
7534                segtree.update(1,1,n,cur - l[u]+1,cur - l[up_to[cur]],-1);
8094                swap(up_to[cur],u);
95cf            }
1262            dfstree.update(1,1,cnt,in[now],i);
82e3            up_to[i] = 1;
d537            while (!query.empty() and query.back().first.second == i){
ba5e                int l = query.back().first.first;
778a                int id = query.back().second;
931e                ans[id] = segtree.query(1,1,n,l,i);
cdbf                query.pop_back();
95cf            }
95cf        }
95cf    }
5eed}sam;
3117int main(){
9c97    cin>>n>>q;
499d    cin>>s+1;
3eb4    sam.init(s+1);
949d    for (int i=1;i<=q;i++){
9f6b        int l,r;
ad6f        cin>>l>>r;
735a        query.push_back({{l+1,r+1},i});
95cf    }
a4ee    sort(query.begin(),query.end(),[](Query x,Query y){
3fd9        return x.first.second > y.first.second;
b251    });
1923    sam.gao();
949d    for (int i=1;i<=q;i++){
ccb3        cout<<ans[i]<<endl;
95cf    }
7021    return 0;
95cf}
```

3 Algorithm

3.1 Geometry

```
302f#include <bits/stdc++.h>
421cusing namespace std;
ce18const int maxn = 10000 + 50;
```

```
320e template<class type>
9704 struct point{
ce03     type x,y;
5cb2     point(){};
f40a     point(type x_,type y_):x(x_),y(y_){}
f510     point operator +(const point &p)const {return point(x + p.x,y + p.y);}
3ecb     point operator -(const point &p)const {return point(x - p.x,y - p.y);}
427e     //a related to b
427e     //clockwise : positive
427e     //anti-clockwise : negative
427e     //share a line : zero
dce3     type cross(const point &p)const {return x * p.y - y * p.x;}
a809     type dot(const point &p)const {return x * p.x + y * p.y;}
2f3a     type cross(const point &a,const point &b)const {return (a - *this).cross(b -
             *this);}
7f6b     type dot(const point &a,const point &b)const {return (a - *this).dot(b - *
           this);}
d92f     type sqrLen()const{return this->dot(*this);}
5bed     type sqrDis(const point &p)const {return (p - *this).sqrLen();}
329b };
d7b8 typedef point<long long> pt;
9d10 namespace Geometry{
fd78     const double PI = acos(-1.0);
427e     //res[0]: left most and bottom most
427e     //anti-clockwise
427e     //no three points share one line
427e     //WARN: this function modifies points
2325     vector<pt> Convex_Hull(vector<pt> &points){
8fa3         vector<pt> res(0);
0ca4         assert(points.size() >= 3);
bf80         int idx = 0;
6281         for (int i=1;i<points.size();i++){
28dc             pt temp = points[i];
a34c             pt now = points[idx];
4897             if (temp.x < now.x || temp.x == now.x && temp.y < now.y)idx = i;
95cf         }
8d08         swap(points[idx],points[0]);
9837         sort(points.begin()+1,points.end(),[&](pt x,pt y){
89c2             double cro = points[0].cross(x,y);
69ef             if (cro != 0)return cro > 0;
180e             return points[0].sqrDis(x) < points[0].sqrDis(y);
b251         });
7271         res.push_back(points[0]);
c57e         res.push_back(points[1]);
8316         for (int i=2;i<points.size();i++){
b7b9             pt now = points[i];
b94e             while (res.size() >= 2){
df0d                 double cro = res[res.size()-2].cross(now,res.back());
f72d                 auto p = res[res.size()-2];
e810                 auto pp = res.back();
63f2                 if (cro >= 0)res.pop_back();
caf8                 else break;
95cf             }
49f1             res.push_back(now);
95cf         }
244d         return res;
95cf     }
427e     //calc the Minkowski Sum of two Convex Hull
d0a9     vector<pt> Minkowski(const vector<pt> &ch1,const vector<pt> &ch2){
ef50         assert(ch1.size() >= 3);
ff7e         assert(ch2.size() >= 3);
7c15         stack<pt> vec1;
ee2b         stack<pt> vec2;
7245         for (int i = ch1.size() - 1;i >=0;i--){
a9f5             vec1.push(ch1[(i+1)%ch1.size()] - ch1[i]);
95cf         }
3cde         for (int i = ch2.size() - 1;i >= 0;i--){
6f4f             vec2.push(ch2[(i+1)%ch2.size()] - ch2[i]);
95cf         }
8fa3         vector<pt> res(0);
2219         res.push_back(ch1.front() + ch2.front());
186a         while (!vec1.empty() && !vec2.empty()){
b518             auto v1 = vec1.top();
f296             auto v2 = vec2.top();
dca9             long long cro = v1.cross(v2);
6b8d             if (cro > 0){
0c49                 res.push_back(res.back() + v1);
cb19                 vec1.pop();
8e2e             }else{
0ea2                 res.push_back(res.back() + v2);
fe8d                 vec2.pop();
95cf             }
95cf         }
6ca4         while (!vec1.empty())res.push_back(res.back() + vec1.top()),vec1.pop();
b356         while (!vec2.empty())res.push_back(res.back() + vec2.top()),vec2.pop();
1f73         return Convex_Hull(res);
95cf     }
427e     //logn
```

```
427e    //wether point in or on convex hull
a023    bool within(pt p,const vector<pt> &ch){
0c3b        assert(ch.size() >= 3);
5221        auto base = ch.front();
d6e7        if (base.cross(p,ch[1]) > 0 || base.cross(p,ch.back()) < 0)return false;
684c        if (base.cross(p,ch[1]) == 0 && (p - base).sqrLen() <= (ch[1] - base).
              sqrLen())return true;
265b        auto cmp = [&](const pt x,const pt y){
d8cd            long long cro = base.cross(x,y);
61b4            return cro>0;
329b        };
d4ae        int i = lower_bound(ch.begin(),ch.end(),p,cmp) - ch.begin() - 1;
8132        int j = i+1;
635b        assert(j < ch.size());
c740        return ch[i].cross(ch[j],p) >= 0;
95cf    }
329b};
```

3.2 Max Flow

```
427e// Created by calabash_boy on 18-9-14.
302f#include<bits/stdc++.h>
421c using namespace std;
4085 typedef long long ll;
32d7 const int maxn = 11000;
3378 const int maxm = 110000;
08a4 const int INF = 0x3f3f3f3f;
5650 struct Max_Flow{
f1b1     int first[maxn],nxt[maxm*2],des[maxm*2],c[maxm*2],tot;
4e95     int dep[maxn];int ss,tt;
b376     Max_Flow(){ clear(); }
1126     void clear(){
4e61         memset(first,-1,sizeof first);tot =-1;
95cf     }
4a69     inline void addEdge(int u,int v,int w){
71cf         tot++;
73e4         des[tot] = v;c[tot] =w;
6570         nxt[tot] = first[u];first[u] = tot;
95cf     }
1836     bool bfs(){
d568         memset(dep,-1,sizeof dep);
0881         dep[ss] =0;
fc6b         queue<int> Q;Q.push(ss);
11e5         while (!Q.empty()){
d7b1             int q = Q.front();Q.pop();
9c72             for (int t = first[q];t!=-1;t= nxt[t]){
b7bb                 int v = des[t],cx = c[t];
c804                 if (dep[v]==-1&&cx){
31e8                     dep[v] = dep[q]+1;
78e5                     Q.push(v);
95cf                 }
95cf             }
95cf         }
45fe         return dep[tt]!=-1;
95cf     }
c29e     int dfs(int node,int now){
0031         if (node==tt)return now;
5839         int res =0;
1e7e         for (int t = first[node];t!=-1&&res<now;t=nxt[t]){
b7bb             int v = des[t],cx = c[t];
da1a             if (dep[v]==dep[node]+1&&cx){
223c                 int x = min(cx,now-res);
6c2e                 x = dfs(v,x);
29d4                 res+=x;c[t]-=x;c[t^1]+=x;
95cf             }
95cf         }
7399         if (!res) dep[node] = -2;
244d         return res;
95cf     }
427e     // tuple<from,to,flow>
4649     void init(vector<tuple<int,int,int> > Edge){
1cbd         for (auto tp : Edge){
1de2             int u,v,w;tie(u,v,w) = tp;
16fe             addEdge(u,v,w);addEdge(v,u,0);
95cf         }
95cf     }
427e     // s->t max_flow
9783     ll max_flow(int s,int t){
8786         ss = s;tt = t;
692e         ll res =0,del =0;
75d3         while (bfs()){while (del = dfs(ss,INF)){res += del;}}
244d         return res;
95cf     }
8596 }net;
4dbf int n,m,s,t;
8f52 vector<tuple<int,int,int> > E;
```

```
3117 int main(){
5dae     scanf("%d%d%d%d",&n,&m,&s,&t);
356f     for (int i=0;i<m;i++){
3676         int u,v,w;
95a1         scanf("%d%d%d",&u,&v,&w);
be22         E.push_back(make_tuple(u,v,w));
95cf     }
08d9     net.init(E);
9560     printf("%lld\n",net.max_flow(s,t));
7021     return 0;
95cf }
```

3.3 Min Cost Max Flow(Min Cost Flow)

```
427e
427e // Created by calabash_boy on 19-10-5.
302f #include <bits/stdc++.h>
421c using namespace std;
6cca const int maxn = 3 * 250 + 100;
1517 const int maxm = 2 * 250 * 250 + 100;
b9bf const int inf = 10000;
08a4 const int INF = 0x3f3f3f3f;
c6cb struct MCMF{
5217     int ss,tt,dis[maxn],pre[maxn];
4b98     int first[maxn],from[maxm*2],des[maxm*2],nxt[maxm*2],cost[maxm*2],flow[maxm
           *2],tot;
e50d     bool in[maxn];
2826     MCMF(){
1d56         clear();
95cf     }
1126     void clear(){
ee65         tot =-1;
8eac         memset(first,-1,sizeof first);
95cf     }
427e     // <u,v,flow,cost>
d399     void init(vector<tuple<int,int,int,int> > E){
757c         for (auto edge : E){
4240             int u,v,f,c;
231d             tie(u,v,f,c) = edge;
b841             addEdge(u, v, f, c);
95cf         }
95cf     }
```

```
dbb4 void __addE(int x,int y,int f,int c){
71cf     tot++;
575f     from[tot] =x;des[tot] =y;
4b45     flow[tot] =f;cost[tot] =c;
6d84     nxt[tot] = first[x];first[x] = tot;
95cf }
f1f8 inline void addEdge(int x,int y,int f,int c){
f355     __addE(x,y,f,c);__addE(y,x,0,-c);
95cf }
3c52 bool spfa(){
f25d     memset(in,0,sizeof in);
a9d8     for (int i=0;i<maxn;i++)dis[i] = INF;
56b2     memset(pre,-1,sizeof pre);
9669     dis[ss] =0;in[ss] =1;
fc6b     queue<int> Q;Q.push(ss);
11e5     while (!Q.empty()){
3b29         int q = Q.front();
f56a         Q.pop();in[q] = 0;
9c72         for (int t = first[q];t!=-1;t = nxt[t]){
4993             int v=des[t],len=cost[t],cx=flow[t];
50ae             if (cx&&dis[v]>dis[q]+len){
e29b                 dis[v] = dis[q]+len;
0986                 pre[v] = t;
7476                 if (!in[v]){
d143                     Q.push(v);in[v] = 1;
95cf                 }
95cf             }
95cf         }
95cf     }
427e     // min cost max flow
427e     //return pre[tt] != -1;
427e
427e     // min cost. flow needn't be max.
5287     return pre[tt]!=-1 && dis[tt] < 0;
95cf }
427e // <flow,cost>
ae82 pair<int,int> run(int s, int t){
8786     ss =s;tt=t;
eb96     int totflow =0,totcost =0,nowflow =0,nowcost =0;
22dc     while (spfa()){
2c90         nowcost =0;nowflow = INF;
d3ff         int now =pre[tt];
21b8         while (now!=-1){
f5f6             nowflow = min(nowflow,flow[now]);
```

```
61af                now = pre[from[now]];
95cf            }
83dd            now = pre[tt];
21b8            while (now!=-1){
1839                flow[now] -= nowflow;
fee0                flow[now^1] += nowflow;
96be                nowcost +=cost[now];
61af                now = pre[from[now]];
95cf            }
db07            nowcost*=nowflow;
9bc4            totflow +=nowflow;
0178            totcost +=nowcost;
95cf        }
9589        return make_pair(totflow,totcost);
95cf    }
427e    // special
0abd    void output(int cost);
70ae }mcmf;
35b8 int n,m;
8960 int a[maxn];
e8ac int id[maxn];
5718 int argvalue[maxn];
a300 vector<string> ans;
c056 void copy(int argid,int val){
3970     stringstream stm;
2fb3     stm<<(char)('a' + argid - 1)<<"="<<val;
e0f6     ans.push_back(stm.str());
95cf }
2def void print(int argid){
3970     stringstream stm;
ab5f     stm<<"print("<<(char)('a' + argid - 1)<<")";
e0f6     ans.push_back(stm.str());
95cf }
5273 void MCMF::output(int cost){
610d     int argid = 0;
6dbf     for (int i=1;i<=n;i++){
3db1         int A = 2 * i-1;
fe76         int B = 2 * i;
3979         if (id[A] == 0){
dbc5             argid ++;
c40b             id[A] = argid;
a4ca             copy(argid, a[i]);
9257             print(argid);
79a3             argvalue[argid] = a[i];
8e2e         }else{
2c77             int temp_value = argvalue[id[A]];
080d             if (temp_value != a[i]){
16e6                 copy(id[A], a[i]);
8c83                 argvalue[id[A]] = a[i];
95cf             }
b391             print(id[A]);
95cf         }
2516         for (int t = first[B];t != -1;t = nxt[t]){
e8e0             int v = des[t];
2bc8             int f = flow[t];
c8f5             if (f|| v == A){
b333                 continue;
95cf             }
f914             if (v == 2 * n + 3) break;
037f             else{
8919                 id[v] = id[A];
95cf             }
95cf         }
95cf     }
6f76     cout<<ans.size()<<"␣"<<cost<<endl;
03de     for (auto str : ans){
cc6d         cout<<str<<endl;
95cf     }
95cf }
3117 int main(){
9af0     cin>>n>>m;
6dbf     for (int i=1;i<=n;i++){
879c         cin>>a[i];
95cf     }
efbd     vector<tuple<int,int,int,int> > E(0);
f385     int SS = 2 * n + 1;
dc84     int S = 2 * n + 2;
c8df     int T = 2 * n + 3;
6962     E.push_back(make_tuple(SS,S,m,0));
6dbf     for (int i=1;i<=n;i++){
3db1         int A = 2 * i - 1;
fe76         int B = 2 * i;
3531         E.push_back(make_tuple(A,B,1,-inf));
1cb5         E.push_back(make_tuple(S,A,1,__builtin_popcount(a[i])));
0673         E.push_back(make_tuple(B,T,1,0));
ed35         for (int j=i+1;j<=n;j++){
71ea             int AA = 2 * j - 1;
1e22             int BB = 2 * j;
```

```
            if (a[i] == a[j]){
                E.push_back(make_tuple(B,AA,1,0));
            }else{
                E.push_back(make_tuple(B,AA,1,__builtin_popcount(a[j])));
            }
        }
    }
    mcmf.init(E);
    pair<int,int> ans = mcmf.run(SS, T);
    //cerr<<ans.first<<","<<ans.second<<endl;
    mcmf.output((ans.second% inf + inf) % inf);
    return 0;
}
```

3.4 LCA

```
// Created by calabash_boy on 18-7-7.
#include<bits/stdc++.h>
using namespace std;
const int maxn = 5e5+100;
int first[maxn],des[maxn*2],nxt[maxn*2],tot;
int n,m,s;
inline int addEdge(int x,int y){
    tot++;des[tot] = y;
    nxt[tot] = first[x];
    first[x] = tot;
}
namespace Multiply_LCA{
    int fa[maxn][20],dep[maxn];
    void dfs(int u,int father){
        fa[u][0] = father;
        dep[u] = dep[father]+1;
        for (int i=1;i<20&&fa[u][i-1];i++){
            fa[u][i] = fa[fa[u][i-1]][i-1];
        }
        for (int t=first[u];t;t=nxt[t]){
            int v = des[t];
            if (v==father)continue;
            dfs(v,u);
        }
    }
    int lca(int x,int y){
        if (dep[x]<dep[y])swap(x,y);
        for (int i=19;i>=0;i--){
            if (dep[fa[x][i]]>=dep[y]){
                x = fa[x][i];
            }
        }
        if (x==y)return x;
        for (int i=19;i>=0;i--){
            if (fa[x][i]!=fa[y][i]){
                x = fa[x][i];
                y = fa[y][i];
            }
        }
        return fa[y][0];
    }
};
int main(){
    scanf("%d%d%d",&n,&m,&s);
    for (int i=1;i<n;i++){
        int x,y;
        scanf("%d%d",&x,&y);
        addEdge(x,y);addEdge(y,x);
    }
    Multiply_LCA::dfs(s,0);
    while (m--){
        int x,y;scanf("%d%d",&x,&y);
        printf("%d\n",Multiply_LCA::lca(x,y));
    }
    return 0;
}
```

3.5 DSU On Tree

```
// Created by calabash_boy on 18-10-8.
// 1-rooted tree
// query vertex with height H in subtree of V
// whether the letter can form a palindrome
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
typedef pair<int,int> pii;
#define rep(i,l,r) for (ll i = l,_ = r;i< _;i++)
```

```
5879 #define REP(i,l,r) for (ll i=l,_=r;i<=_;i++)
6f64 const int maxn = 5e5+100;
2ff9 int n,tot,first[maxn],des[maxn],nxt[maxn],m;
28d5 vector<pii> Q[maxn];
f96d int cnt[maxn][26],Cnt[maxn];
bbe3 int sz[maxn],dep[maxn],wson[maxn];
f0f2 bool ans[maxn],big[maxn];
15df char s[maxn];
453e inline void addEdge(int x,int y){
4704     tot++;des[tot] = y;
465b     nxt[tot] = first[x];
86fa     first[x] = tot;
95cf }
0d39 void get_sz(int node,int depth){
2b42     dep[node] = depth;sz[node] = 1;
e83e     for (int t = first[node];t;t=nxt[t]){
e8e0         int v = des[t];
a0d5         get_sz(v,depth+1);
47d5         sz[node] += sz[v];
03ee         if (sz[v] > sz[wson[node]])wson[node] = v;
95cf     }
95cf }
5efd void add(int node,int sign){
b01b     Cnt[dep[node]] -= cnt[dep[node]][s[node]-'a'];
d2e8     cnt[dep[node]][s[node]-'a'] ^=1;
937f     Cnt[dep[node]] += cnt[dep[node]][s[node]-'a'];
e83e     for (int t = first[node];t;t=nxt[t]){
e8e0         int v = des[t];
dcb7         if (big[v])continue;
ec6e         add(v,sign);
95cf     }
95cf }
5cc1 void dfs(int node,bool keep){
e83e     for (int t = first[node];t;t=nxt[t]){
e8e0         int v = des[t];
5279         if (v == wson[node])continue;
4bc1         dfs(v,0);
95cf     }
d010     if (wson[node]){
6048         big[wson[node]]=1;
11b7         dfs(wson[node],1);
95cf     }
7111     add(node,1);
3a0c     for (auto q:Q[node]){
1c95         ans[q.second] = Cnt[q.first] <=1;
95cf     }
918e     if (wson[node])big[wson[node]] = 0;
dc2a     if (!keep)add(node,-1);
95cf }
3117 int main(){
ac98     scanf("%d%d",&n,&m);
eeaf     REP(i,2,n){
4ec4         int p;
e75e         scanf("%d",&p);
be80         addEdge(p,i);
95cf     }
a275     scanf("%s",s+1);
a826     rep(i,0,m){
8213         int v,h;
fdd4         scanf("%d%d",&v,&h);
3e7f         Q[v].push_back({h,i});
95cf     }
ff05     get_sz(1,1);dfs(1,0);
8823     rep(i,0,m)printf("%s\n",ans[i]?"Yes":"No");
7021     return 0;
95cf }
```

4 Data Structure

4.1 01 Trie

```
427e // Created by calabash_boy on 18-7-7.
427e // max(XorSum(a_l^r))
302f #include<bits/stdc++.h>
421c using namespace std;
ed66 const int MAX = 1e6+100;
80de int bas[35],n,Cas;
92ad const int INF = 2147483645;
a281 struct Trie{
abd0     int nxt[MAX<<2][2],l[MAX<<2];
a945     int cnt,ansl,ansr,ansv;
5d53     void init(){
68de         cnt =ansv = 0;
16d8         memset(nxt[0],0,sizeof (nxt[0]));
aa76         memset(l,0x3f3f3f3f,sizeof(l));
95cf     }
```

```
    int create(){
        cnt++;
        memset(nxt[cnt],0,sizeof (nxt[cnt]));
        return cnt;
    }
    void insert(int id,int x){
        int y = 0;
        for (int i=30;i>=0;i--){
            int t = x&bas[i];
            t>>=i;
            if (!nxt[y][t])nxt[y][t] = create();
            y = nxt[y][t];
        }
        l[y] = min(l[y],id);
    }
    void query(int id,int x){
        int y=0;  int res =0;
        for (int i=30;i>=0;i--){
            int t = x&bas[i];
            t>>=i;
            if (nxt[y][!t]){
                y =nxt[y][!t];
                res+=bas[i];
            }else{
                y = nxt[y][t];
            }
        }
        if (res==ansv){
            if (l[y]<ansl){
                ansl = l[y];  ansr = id;
            }
        }else if (res>ansv){
            ansv = res;
            ansl = l[y];
            ansr = id;
        }
    }
}trie;
int main(){
    bas[0] = 1;
    for (int i1=1;i1<=30;i1++)bas[i1] = bas[i1-1]<<1;
    scanf("%d",&Cas);
    for (int i=1;i<=Cas;i++){
        trie.init();  trie.insert(0,0);
        scanf("%d",&n);
        int sum=0;
        for (int j=1;j<=n;j++){
            int ai;
            scanf("%d",&ai);  sum^=ai;
            trie.query(j,sum);  trie.insert(j,sum);
        }
        printf("Case #%d:\n%d %d\n", i, trie.ansl + 1, trie.ansr);
    }
    return 0;
}
```

4.2 Cartesian Tree

```
// Created by calabash_boy on 18-7-24.
//他的名字是笛卡尔树。
#include<bits/stdc++.h>
using namespace std;
#define OPENSTACK
const int maxn = 1e6+100;
const int mod = 1e9+7;
typedef long long LL;
int stk[maxn],top,sz[maxn];
int l[maxn],r[maxn],rt,n;
pair<int,int> a[maxn];
LL inv[maxn],fac[maxn],inv_fac[maxn];
bool vis[maxn];
/* l 左儿子 r 右儿子 rt根*/
void build(){
    top=0;
    for (int i=1;i<=n;i++) l[i]=r[i]=vis[i] =0;
    for (int i=1;i<=n;i++){
        int k = top;
        while (k&&a[i]<a[stk[k-1]])k--;
        if (k) r[stk[k-1]] = i;
        if (k<top) l[i] = stk[k];
        stk[k++] =i;top = k;
    }
    for (int i=1;i<=n;i++) vis[l[i]] = vis[r[i]] =1;
    for (int i=1;i<=n;i++){
        if (!vis[i]){
            rt = i;
```

```
6173            break;
95cf        }
95cf    }
95cf}
a89aLL power(LL x,LL y){
0aee    LL res =1;
db1a    while (y){
349b        if (y&1)res = res*x%mod;
af39        y>>=1;
df96        x = x*x%mod;
95cf    }
244d    return res;
95cf}
0f81inline LL C(int n,int m){
54dd    return fac[n]*inv_fac[m]%mod*inv_fac[n-m]%mod;
95cf}
f33fint dfs(int u){
fdf8    sz[u]=1;int ans =1;
fe92    if (l[u])ans=1LL*ans*dfs(l[u])%mod;
429f    if (r[u])ans = 1LL*ans*dfs(r[u])%mod;
2c7a    sz[u]+=sz[l[u]]+sz[r[u]];
b778    return 1LL*ans*C(sz[u]-1,sz[l[u]])%mod;
95cf}
6e6dvoid Main(){
acce    inv[1]=fac[1]=fac[0]=1;
3295    for (int i=2;i<maxn;i++)fac[i] = fac[i-1]*i%mod,inv[i] = inv[mod%i]*(mod-mod
          /i)%mod;
5f9e    inv_fac[maxn-1] = power(fac[maxn-1],mod-2);
c2aa    for (int i=maxn-2;i>=0;i--){
4cf8        inv_fac[i] = inv_fac[i+1]*(i+1)%mod;
95cf    }
d6b7    int T;scanf("%d",&T);
60ca    while (T--) {
cd91        scanf("%d", &n);
6dbf        for (int i = 1; i <= n; i++) {
7681            int x;scanf("%d", &x);
d6d4            a[i] = {-x, i};
95cf        }
7068        build();
b475        printf("%d\n", inv[2] * n % mod * power(fac[n], mod - 2) % mod * dfs(rt)
              % mod);
95cf    }
95cf}
3117int main(){
```

```
4b95#ifdef OPENSTACK
90c5    int size = 70 << 20; // 256MB
9efa    char *p = (char*)malloc(size) + size;
8c82#if (defined _WIN64) or (defined __unix)
665b    __asm__("movq␣%0,␣%%rsp\n" :: "r"(p));
a8cb#else
355e    __asm__("movl␣%0,␣%%esp\n" :: "r"(p));
1937#endif
1937#endif
362c    Main();
4b95#ifdef OPENSTACK
a398    exit(0);
a8cb#else
7021    return 0;
1937#endif
95cf}
```

4.3 Chairman Tree

```
427e// Created by calabash_boy on 18-7-7.
427e// query_kth_element
302f#include<bits/stdc++.h>
421cusing namespace std;
52c1const int maxn=1e5+100;
b425int a[maxn];int rk[maxn];int pos[maxn];
15acint root[maxn];int cnt,m,n,T;
6207struct Chairman_Tree{
108d    struct Node{int L,R,val;}tree[maxn*500];
5d53    void init(){
a4f5        memset(root,0,sizeof root);
8766        cnt =0;
95cf    }
94cf    /* 建T0空树 */
cf84    int buildT0(int l, int r){
64f2        int k = cnt++;
e9d1        tree[k].val =0;
eb40        if (l==r) return k;
b8b7        int mid = l+r >>1;
1e97        tree[k].L = buildT0(l, mid);tree[k].R = buildT0(mid + 1, r);
e27b        return k;
95cf    }
e965    /* 上一个版本节点P，【ppos】+=del 返回新版本节点*/
```

```
3a6b     int update (int P,int l,int r,int ppos,int del){
64f2         int k = cnt++;
1e22         tree[k].val = tree[P].val +del;
eb40         if (l==r) return k;
b8b7         int mid = l+r >>1;
4af7         if (ppos<=mid){
59bb             tree[k].L = update(tree[P].L,l,mid,ppos,del);
1cb7             tree[k].R = tree[P].R;
8e2e         }else{
a8f5             tree[k].L = tree[P].L;
d096             tree[k].R = update(tree[P].R,mid+1,r,ppos,del);
95cf         }
e27b         return k;
95cf     }
4798     int query_kth(int lt,int rt,int l,int r,int k){
9e61         if (l==r) return a[rk[l]];
b8b7         int mid = l+r >>1;
9988         if (tree[tree[rt].L].val-tree[tree[lt].L].val>=k) return query_kth(tree[
               lt].L,tree[rt].L,l,mid,k);
38e4         else return query_kth(tree[lt].R,tree[rt].R,mid+1,r,k+tree[tree[lt].L].
               val-tree[tree[rt].L].val);
95cf     }
b0c1 }tree;
56b1 bool cmp(int x,int y){return a[x]<a[y];}
3117 int main() {
1fd9     scanf("%d", &T);
60ca     while (T--) {
ac98         scanf("%d%d",&n,&m);
6dbf         for (int i=1;i<=n;i++){
9a1c             scanf("%d",&a[i]);
f9d0             rk[i]=i;
95cf         }
a475         tree.init();
f0ca         sort(rk+1,rk+1+n,cmp);
8b31         for (int i1=1;i1<=n;i1++){
9b5e             pos[rk[i1]] =i1;
95cf         }
b6a2         root[0] = tree.buildT0(1, n);
8b31         for (int i1=1;i1<=n;i1++){
8294             root[i1] = tree.update(root[i1-1],1,n,pos[i1],1);
95cf         }
3f3a         while (m--){
d32c             int l,r,k;scanf("%d%d%d",&l,&r,&k);
26ab             printf("%d\n",tree.query_kth(root[l-1],root[r],1,n,k));
95cf         }
95cf     }
7021     return 0;
95cf }
```

4.4 KD Tree

```
427e // Created by calabash_boy on 18-10-6.
302f #include<bits/stdc++.h>
421c using namespace std;
5cad typedef long long LL;
eb45 const int maxn = 2e5+100;
b1ec const LL INF = 0x3f3f3f3f3f3f3f3fLL;
4d9b int m,n;
fc74 const int demension = 2;
4825 struct Hotel{
b199     int pos[demension],id,c;
4922 }hotel[maxn],kdtree[maxn];
2ece double var[demension];
8003 int split [maxn];int cmpDem;
5cdc bool cmp(const Hotel &a,const Hotel &b){
b5cd     return a.pos[cmpDem]<b.pos[cmpDem];
95cf }
d5af void build (int l,int r){
2625     if (l>=r)return;
b8b7     int mid = l+r >>1;
8037     for (int i=0;i<demension;i++){
4655         double ave =0;
a0d3         for (int j=l;j<=r;j++){
70b6             ave+=hotel[j].pos[i];
95cf         }
b1eb         ave/=(r-l+1);var[i] =0;
a0d3         for (int j=l;j<=r;j++){
27fe             var[i]+=pow(hotel[j].pos[i]-ave,2);
95cf         }
6e08         var[i]/=(r-l+1);
95cf     }
3909     split[mid] =-1;double maxVar=-1;
8037     for (int i=0;i<demension;i++){
d704         if (var[i]>maxVar){
3bdc             maxVar = var[i];
9c04             split[mid] =i;
```

```
        }
    }
    cmpDem = split[mid];
    nth_element(hotel+l,hotel+mid,hotel+r+1,cmp);
    build (l,mid-1);build (mid+1,r);
}
int ansIndex;
LL ansDis;
void query(int l,int r,const Hotel& x){
    if (l>r)return ;
    int mid = l+r >>1;LL dis =0;
    for (int i=0;i<demension;i++){
        dis +=1LL*(x.pos[i]-hotel[mid].pos[i])*(x.pos[i]-hotel[mid].pos[i]);
    }
    if (hotel[mid].c<=x.c){
        if (ansDis == dis && hotel[mid].id<hotel[ansIndex].id){
            ansIndex = mid;
        }else if (dis<ansDis){
            ansDis = dis;
            ansIndex = mid;
        }
    }
    int d = split[mid];
    LL radius = 1LL*(x.pos[d]-hotel[mid].pos[d])*(x.pos[d]-hotel[mid].pos[d]);
    if (x.pos[d]<hotel[mid].pos[d]){
        query(l,mid-1,x);
        if (ansDis>radius){query(mid+1,r,x);}
    }else{
        query(mid+1,r,x);
        if (ansDis>radius){query(l,mid-1,x);}
    }
}
int T;
void input(){
    scanf("%d%d",&n,&m);
    for (int i=0;i<n;i++){
        scanf("%d%d%d",&hotel[i].pos[0],&hotel[i].pos[1],&hotel[i].c);
        hotel[i].id=i;
    }
    build (0,n-1);
}
void solve(){
    Hotel x;
    for (int i=1;i<=m;i++){
        scanf("%d%d%d",&x.pos[0],&x.pos[1],&x.c);
        ansDis = INF;ansIndex =n+1;
        query(0,n-1,x);
        printf("%d␣%d␣%d\n",hotel[ansIndex].pos[0],hotel[ansIndex].pos[1],hotel[
          ansIndex].c);
    }
}
int main(){
    scanf("%d",&T);
    while (T--){
        input();
        solve();
    }
    return 0;
}
```

4.5 Segment Tree

```
// Created by calabash_boy on 18-9-14.
// interval modify & interval query
#include<stdio.h>
using namespace std;
const int maxn = 1e5+100;
typedef long long LL;
int a[maxn];
struct Seg_Tree{
    LL val[maxn*4];LL lazy[maxn*4];
    inline void Up(int x){val[x] = val[x<<1]+val[x<<1|1];}
    inline void Down(int x,int l,int mid,int r){
        if (lazy[x]){
            val[x<<1] += 1LL*lazy[x]*(mid-l+1);
            val[x<<1|1] += 1LL*lazy[x]*(r-mid);
            lazy[x<<1]+= lazy[x];
            lazy[x<<1|1] += lazy[x];
            lazy[x] =0;
        }
    }
    void build (int x,int l,int r){
        lazy[x] =0;
        if (l==r){val[x] = a[l];return ;}
        int mid = l+r >>1;
        build (x<<1,l,mid);build (x<<1|1,mid+1,r);
```

```
8eb6        Up(x);
95cf    }
f3fe    void add(int x,int l,int r,int L,int R,int del){
2fdc        if (l>R||r<L)return;
4d29        if (L<=l&&r<=R){
6171            val[x]+=1LL*del*(r-l+1);
1eeb            lazy[x]+=del;
4f2d            return;
95cf        }
b8b7        int mid = l+r >>1;
4dc2        Down(x,l,mid,r);
5468        add(x<<1,l,mid,L,R,del);add(x<<1|1,mid+1,r,L,R,del);
8eb6        Up(x);
95cf    }
073d    LL query_Sum(int x,int l,int r,int L,int R){
0872        if (l>R||r<L)return 0;
26cd        if (L<=l&&r<=R)return val[x];
b8b7        int mid = l+r >>1;
4dc2        Down(x,l,mid,r);
1fb2        return query_Sum(x<<1,l,mid,L,R)+query_Sum(x<<1|1,mid+1,r,L,R);
95cf    }
b0c1 }tree;
3d22 char opt[5];int m,n;
3117 int main(){
ac98    scanf("%d%d",&n,&m);
6dbf    for (int i=1;i<=n;i++){
60cb        scanf("%d",a+i);
95cf    }
e703    tree.build(1,1,n);
3f3a    while (m--){
42ba        int l,r,v;
e158        scanf("%s%d%d",opt,&l,&r);
0d1b        if (opt[0]=='Q'){
b8ef            printf("%I64d\n",tree.query_Sum(1,1,n,l,r));
ff96        }else if (opt[0]=='C'){
a9ba            scanf("%d",&v);
b937            tree.add(1,1,n,l,r,v);
95cf        }
95cf    }
7021    return 0;
95cf }
```

4.6 AFL(Cactus)

```
427e // Created by calabash_boy on 18-9-14.
427e // circle-square-tree Maximum independent set
302f #include<bits/stdc++.h>
421c using namespace std;
52c1 const int maxn = 1e5+100;
9010 vector<int> E1[maxn],ET[maxn];
c940 int m,n,N,fa[maxn],dp[maxn][2];
d746 int len[maxn],dfn[maxn],dfs_clock;
e6da bool inCircle[maxn];
4ab4 int dp2[maxn][2];
e227 inline void addEdge1(int x,int y){
f4a7     E1[x].push_back(y);
95cf }
2a27 inline void addEdgeT(int x,int y){
de38     ET[x].push_back(y);
95cf }
0e91 void input(){
64f1     cin>>n>>m;N =n;
356f     for (int i=0;i<m;i++){
97c3         int u,v;cin>>u>>v;
2775         addEdge1(u,v);addEdge1(v,u);
95cf     }
95cf }
74b1 void tarjan(int u){
f5c7     dfn[u] = ++dfs_clock;
1958     for (int i=0;i<E1[u].size();i++){
1654         int v = E1[u][i];
8e32         if (v==fa[u])continue;
3c64         if (!dfn[v]){
da94             fa[v] = u;tarjan(v);
e245         }else if (dfn[v]<dfn[u]){
c93c             n++;
478b             len[n] = dfn[u]-dfn[v]+1;
0f08             fa[n] = v;
92b2             addEdgeT(v,n);
8845             int temp = u;
a7eb             while (temp!=v){
3d33                 inCircle[temp] = true;
96c4                 addEdgeT(n,temp);
6dbe                 temp = fa[temp];
95cf             }
95cf         }
```

```
    }
    if (!inCircle[u]){
        addEdgeT(fa[u],u);
    }
    dfs_clock--;
}
void work(int x){
    int sz = ET[x].size();
    if (sz==2){
        int son1 = ET[x][0];
        int son2 = ET[x][1];
        dp[x][0] = dp[son1][0]+dp[son2][0];
        dp[x][1] = max(dp[son1][0]+dp[son2][0],max(dp[son1][0]+dp[son2][1],dp[
          son1][1]+dp[son2][0]));
        return;
    }
    dp2[0][0] =dp[ET[x][0]][0];dp2[0][1]=0;
    for (int i=1;i<sz;i++){
        dp2[i][0] = max(dp2[i-1][0],dp2[i-1][1])+dp[ET[x][i]][0];
        dp2[i][1] = dp2[i-1][0]+dp[ET[x][i]][1];
    }
    dp[x][0] = dp2[sz-1][0];
    dp[x][1] = dp2[sz-1][0];
    dp2[sz][0]=dp2[sz][1]=0;
    for (int i=sz-1;i>=0;i--){
        dp2[i][0] = max(dp2[i+1][0],dp2[i+1][1])+dp[ET[x][i]][0];
        dp2[i][1] = dp2[i+1][0]+dp[ET[x][i]][1];
    }
    dp[x][1] = max(dp[x][1],max(dp2[0][0],dp2[0][1]));
}
void dfs(int u){
    dp[u][0]=0;dp[u][1]=1;
    if (u>N)dp[u][0]=0;
    for (int i=0;i<ET[u].size();i++){
        int v = ET[u][i];
        dfs(v);
        if (u<=N){
            dp[u][0]+=max(dp[v][1],dp[v][0]);
            dp[u][1]+=dp[v][0];
        }
    }
    if (u>N)work(u);
}
int main(){
    input();
    tarjan(1);
    dfs(1);
    cout<<max(dp[1][0],dp[1][1])<<endl;
    return 0;
}
```

4.7 Segment Tree(Dynamic Memory).cpp

```
// Created by calabash_boy on 18-10-1.
// CF 1046A
// give n tuple(x,r,p) and k<=20 , calc unordered pair(i,j)
// xi - ri <= xj <= xi + ri
// xj - rj <= xi <= xj + rj
// |pi - pj| <=k
#include <bits/stdc++.h>
using namespace std;
const int maxn = 1e5+100;
typedef long long ll;
struct Node{ int L,R,val; }tree[maxn*200];
int cnt;
struct Segment_Tree{
    int root = 0;
    int newnode(){
        ++cnt;
        tree[cnt].val = tree[cnt].L = tree[cnt].R = 0;
        return cnt;
    }
    Segment_Tree(){ root = newnode(); }
    void add(int x,int l,int r,int Pos,int delta){
        tree[x].val += delta;
        if (l == r)return;
        int mid = l+r >>1;
        if (Pos <= mid){
            if (tree[x].L == 0){
                tree[x].L = newnode();
            }
            add(tree[x].L,l,mid,Pos,delta);
        }else{
            if (tree[x].R == 0){
                tree[x].R = newnode();
            }
```

```
492e            add(tree[x].R,mid+1,r,Pos,delta);
95cf        }
95cf    }
30b1    int query(int x,int l,int r,int L,int R){
52df        if (!x)return 0;
b8e7        if (l>R || L>r)return 0;
c450        if (L <= l && r <= R)return tree[x].val;
b8b7        int mid = l+r >>1;
b018        return query(tree[x].L,l,mid,L,R) + query(tree[x].R,mid+1,r,L,R);
95cf    }
329b};
9c0b map<int,Segment_Tree> mp;
9a6f map<int,int> id;
d7af int N;
3117 int main(){
232a    int n,k;
9927    scanf("%d%d",&n,&k);
ad91    vector<tuple<int,int,int> > a(n);
7739    vector<int> nums;
1294    for (int i=0;i<n;i++){
6a6b        int x,r,q;scanf("%d%d%d",&x,&r,&q);
82fb        a[i] = make_tuple(x,r,q);
3bee        nums.push_back(x);
ca6f        nums.push_back(x+r);
4730        nums.push_back(x-r);
95cf    }
19cd    sort(nums.begin(),nums.end());
e5bf    nums.erase(unique(nums.begin(),nums.end()),nums.end());
9e70    for (int i=0;i<nums.size();i++){
9b07        id[nums[i]] = i+1;
95cf    }
34ee    N = nums.size();
4c8a    sort(a.begin(),a.end(),[](const tuple<int,int,int> &a,const tuple<int,int,
          int>&b){
ddfb        return get<1>(a) > get<1>(b);
b251    });
19f3    ll ans =0;
1294    for (int i=0;i<n;i++){
2f4e        int x,r,q;tie(x,r,q) = a[i];
a8aa        int L = id[x-r],R = id[x+r];
af5f        for (int j=q-k;j<=q+k;j++){
7cd6            if (mp.find(j) == mp.end())continue;
8341            Segment_Tree & tree = mp[j];
e7d3            int root = tree.root;
768d            ans += tree.query(root,1,N,L,R);
95cf        }
e2c3        Segment_Tree & tree = mp[q];
e7d3        int root = tree.root;
9252        tree.add(root,1,N,id[x],1);
95cf    }
d592    cout<<ans<<endl;
7021    return 0;
95cf}
```

4.8 Rollback UFS

```
427e //加边删边二部图判定。
302f #include <bits/stdc++.h>
421c using namespace std;
f374 const int maxn = 1e5 + 20;
bd89 struct UFS{
33ef    int fa[maxn];
590c    int sz[maxn];
6873    int len[maxn];
65fd    stack<pair<int*,int> > stk;
5d53    void init(){
e4ba        for (int i=1;i<maxn;i++){
974c            fa[i] = i;
fa1a            sz[i] = 1;
c008            len[i] = 0;
95cf        }
95cf    }
e034    UFS(){
07e2        init();
95cf    }
fee7    pair<int,int> find(int x){
7eb8        if (fa[x] == x)return make_pair(x,0);
037f        else{
2890            pair<int,int> ret = find(fa[x]);
22aa            ret.second ^= len[x];
ee0f            return ret;
95cf        }
95cf    }
427e    // 0 fail
427e    // 1 succ but not update
427e    // 2 succ and update
```

```
41b9     int merge(int x,int y){
7121         int fx,lenx;
5d92         int fy,leny;
9726         tie(fx,lenx) = find(x);
d13a         tie(fy,leny) = find(y);
e94b         if (fx == fy){
4350             return lenx ^ leny;
95cf         }
93ac         if (sz[fx] > sz[fy]){
65b4             swap(lenx,leny);
47d4             swap(x,y);
6c4f             swap(fx,fy);
95cf         }
dfaa         stk.push(make_pair(&sz[fy],sz[fy]));
863a         stk.push(make_pair(&fa[fx],fa[fx]));
a93a         fa[fx] = fy;
24e9         sz[fy] += sz[fx];
3c8a         if (lenx == leny){
5f4d             len[fx] = 1;
8e2e         }else{
7cc4             len[fx] = 0;
95cf         }
ca92         return 2;
95cf     }
831d     void rollback(){
5a7d         for (int i=0;i<2;i++){
503e             int * tar;
d26b             int val;
5b9a             tie(tar,val) = stk.top();
75b6             stk.pop();
9133             (*tar) = val;
95cf         }
427e
95cf     }
5795 }ufs;
58c6 const char* YES = "YES";
a0f7 const char* NO = "NO";
cd1e bool ans[maxn];
23cc struct SegmentTree{
90fc     vector<pair<int,int> > edges[maxn*4];
2161     void put(int x,int l,int r,int L,int R,pair<int,int> e){
d499         if (l > R || L > r)return;
4d29         if (L <= l && r <= R){
5bfc             edges[x].push_back(e);
4f2d             return;
95cf         }
b8b7         int mid = l + r >> 1;
8d76         put(x<<1,l,mid,L,R,e);
36cd         put(x<<1|1,mid+1,r,L,R,e);
95cf     }
8b28     void dfs(int x,int l,int r){
cd24         int succ = true;
8abb         int cnt = 0;
92f7         for (auto e : edges[x]){
0f8b             int x,y;
2bba             tie(x,y) = e;
6848             int ret = ufs.merge(x, y);
ecd5             succ &= ret!= 0;
7c6f             if (!succ){
9102                 for (int i=0;i<cnt;i++)
5e31                     ufs.rollback();
4f2d                 return;
95cf             }
feaf             cnt += ret == 2;
95cf         }
3a0d         if (l == r){
91cd             ans[l] = succ;
9102             for (int i=0;i<cnt;i++)
5e31                 ufs.rollback();
4f2d             return;
95cf         }
b8b7         int mid = l + r >> 1;
7405         dfs(x<<1,l,mid);
b115         dfs(x<<1|1,mid+1,r);
9102         for (int i=0;i<cnt;i++)
5e31             ufs.rollback();
95cf     }
1d91     void debug(int x,int l,int r){
4bde         cerr<<x<<"␣:␣"<<"[␣"<<l<<"␣,␣"<<r<<"␣]"<<endl;
92f7         for (auto e : edges[x]){
54f1             int u,v;
4c70             tie(u,v) = e;
40e5             cerr<<"<␣"<<u<<"␣,␣"<<v<<"␣>"<<endl;
95cf         }
0eec         if (l == r)return;
b8b7         int mid = l + r >> 1;
7dab         debug(x<<1,l,mid);
f599         debug(x<<1|1,mid+1,r);
```

```
95cf     }
f7fb }segtree;
ae0e map<pair<int,int>,vector<int> > mp;
3117 int main(){
1ed7     int n,q;
9c97     cin>>n>>q;
949d     for (int i=1;i<=q;i++){
54f1         int u,v;
a02c         cin>>u>>v;
fd0e         if (u > v)swap(u,v);
7c88         mp[make_pair(u,v)].push_back(i);
95cf     }
957e     for (auto pr : mp){
9660         vector<int> & ts = pr.second;
1e87         if (ts.size() & 1){
a1b6             ts.push_back(q+1);
95cf         }
a8d5         for (int i=0;i<ts.size();i+=2){
7ff9             int st = ts[i];
ab30             int ed = ts[i+1] - 1;
8188             segtree.put(1, 1, q, st, ed, pr.first);
95cf         }
95cf     }
427e     //  segtree.debug(1,1,q);
c9f8     segtree.dfs(1, 1, q);
949d     for (int i=1;i<=q;i++){
9d1d         puts(ans[i]?YES:NO);
95cf     }
7021     return 0;
95cf }
```

4.9 Persistent LiChao SegmentTree

```
427e // Created by calabash_boy on 2019/10/14.
302f #include<bits/stdc++.h>
421c using namespace std;
3045 #define int ll
4085 typedef long long ll;
94c8 const int inf = 1e9 + 5;
2726 const int maxn = 80000 + 50;
9958 const int maxq = 160000 + 50;
80b8 struct Node{
4ae7     int lson,rson,k,b;
427e     //y = k * x + b
5d53     void init(){
d096         lson = rson = 0;
9016         k = b = inf;
95cf     }
abd1 }nodes[maxn * 300];
07b6 int node_cnt = 0;
760d int root[maxn];
55d8 int update(int x,int l,int r,int L,int R,int k,int b){
d06a     int now = node_cnt ++;
2b27     nodes[now] = nodes[x];
b8b7     int mid = l + r >> 1;
0b7f     if (l == L && r == R){
5513         if (k * mid + b < nodes[now].k * mid + nodes[now].b){
98b9             swap(k,nodes[now].k);
0cf6             swap(b,nodes[now].b);
95cf         }
11a1         if (l == r)return now;
419c         if (k * l + b < nodes[now].k * l + nodes[now].b){
e878             nodes[now].lson = update(nodes[x].lson,l,mid,l,mid,k,b);
95cf         }
3833         if (k * r + b < nodes[now].k * r + nodes[now].b){
c91b             nodes[now].rson = update(nodes[x].rson,mid+1,r,mid+1,r,k,b);
95cf         }
7d47         return now;
95cf     }
616e     if (L <= mid)nodes[now].lson = update(nodes[x].lson,l,mid,L,min(mid,R),k,b);
1157     if (mid + 1 <= R)nodes[now].rson = update(nodes[x].rson,mid+1,r,max(mid+1,L)
           ,R,k,b);
7d47     return now;
95cf }
1ed7 int n,q;
b3f9 int a[maxn], b[maxn], c[maxn];
b6a2 vector<int> E[maxn];
312b void dfs(int u,int fa){
6db3     root[u] = update(root[fa],0,inf,0,c[u],b[u],a[u]);
2c0f     for (int v : E[u]){
b6ee         if (v == fa)continue;
e2f7         dfs(v,u);
95cf     }
95cf }
7488 ll query(int x,int l,int r,int pos){
9860     int res = nodes[x].k * pos + nodes[x].b;
```

```
427e    //cerr<<x<<" "<<l<<" "<<r<<":"<<nodes[x].k<<" "<<nodes[x].b<<":"<<pos<<" "<<
          res<<endl;
4745    if (l == r)return res;
b8b7    int mid = l + r >> 1;
e2e9    if (pos <= mid && nodes[x].lson )res = min(res,query(nodes[x].lson,l,mid,pos
          ));
956b    else if (pos > mid &&nodes[x].rson ) res = min(res,query(nodes[x].rson,mid
          +1,r,pos));
244d    return res;
95cf}
3b32signed main(){
1908    scanf("%lld%lld",&n,&q);
6a82    for (int i=1;i<=n;i++)scanf("%lld",a+i);
960d    for (int i=1;i<=n;i++)scanf("%lld",b+i);
d3f4    for (int i=1;i<=n;i++)scanf("%lld",c+i);
324a    for (int i=1;i<n;i++){
54f1        int u,v;
1ddb        scanf("%lld%lld",&u,&v);
068b        E[u].push_back(v);
7e77        E[v].push_back(u);
95cf    }
0c79    root[0] = 0;node_cnt ++;nodes[0].init();
99d6    dfs(1,0);
2cc8    while (q--){
499a        int v,t;
a087        scanf("%lld%lld",&v,&t);
bc8e        printf("%lld\n",query(root[v],0,inf,t));
95cf    }
7021    return 0;
95cf}
```

5 Graph

5.1 Tarjan(BCC of Edge)

```
427e// Created by calabash_boy on 18-10-10.
302f#include<bits/stdc++.h>
421cusing namespace std;
52c1const int maxn = 1e5+100;
5b3fint first[maxn],nxt[maxn*2],from[maxn*2],des[maxn*2],isBrige[maxn*2],tot;
ff12int dfn[maxn],low[maxn],dfs_clock;
8c69int cnt_e[maxn],cnt_n[maxn];int bcc_cnt;
e093bool ok[maxn];vector <int> ans;int m,n;
453einline void addEdge(int x,int y){
71cf    tot++;
56e8    des[tot] =y;from[tot] =x;
6d84    nxt[tot] = first[x];first[x] = tot;
95cf}
0e91void input(){
9af0    cin>>n>>m;
356f    for (int i=0;i<m;i++){
17be        int u,v;scanf("%d%d",&u,&v);
ad4e        addEdge(u,v);addEdge(v,u);
95cf    }
95cf}
312bvoid dfs(int u,int fa){
d413    dfn[u] = low[u] = ++dfs_clock;
3ddf    for (int t = first[u];t;t=nxt[t]){
071c        int v = des[t];if (v==fa)continue;
3c64        if (!dfn[v]){
e2f7            dfs(v,u);
7078            low[u] = min(low[v],low[u]);
f611            if (dfn[u]<low[v]){
4639                isBrige[t] = true;
b158                if (t&1){isBrige[t+1] = true;}
6c47                else{isBrige[t-1] = true;}
95cf            }
e138        }else if (dfn[v]<dfn[u]){low[u] = min(low[u],dfn[v]);}
95cf    }
95cf}
e992void blood_fill(int x){
ec01    dfn[x] = bcc_cnt;
4bb0    for (int t = first[x];t;t=nxt[t]){
9516        if (isBrige[t])continue;
e8e0        int v = des[t];
7127        if (!dfn[v]){blood_fill(v);}
95cf    }
95cf}
fd4bvoid check(){
a599    for (int i=1;i<=n;i++){cnt_n[dfn[i]]++;}
a7c6    for (int i=1;i<=tot;i++){
7701        if (isBrige[i]) continue;
5746        cnt_e[dfn[des[i]]]++;
95cf    }
41ce    for (int i=1;i<=bcc_cnt;i++){
e64d        if (cnt_n[i]*2==cnt_e[i]){ok[i]=1;}
```

```
95cf     }
95cf }
d880 void output(){
8d09     for (int i=1;i<=tot;i+=2){
7701         if (isBrige[i])continue;
c2ef         if (ok[dfn[des[i]]])ans.push_back((i+1)/2);
95cf     }
e139     sort(ans.begin(),ans.end());
c4d5     cout<<ans.size()<<endl;
263e     for (int i=0;i<ans.size();i++){printf("%d ",ans[i]);}
95cf }
9627 void solve(){
c2a0     for (int i=1;i<=n;i++){if (!dfn[i])dfs(i,-1);}
cbec     memset(dfn,0,sizeof dfn);
6dbf     for (int i=1;i<=n;i++){
aa35         if (!dfn[i]){
03f5             bcc_cnt++;
3b53             blood_fill(i);
95cf         }
95cf     }
92ea     check();output();
95cf }
3117 int main(){
2a5c     input();
ccd1     solve();
7021     return 0;
95cf }
```

5.2 Tarjan(BCC of Point)

```
427e // Created by calabash_boy on 18-10-10.
302f #include<bits/stdc++.h>
421c using namespace std;
52c1 const int maxn = 1e5+100;
58a9 int first[maxn],des[maxn*2],nxt[maxn*2],tot;
09ab int bcc_cnt,cnt_n[maxn],cnt_e[maxn],bcc_no[maxn];
ff12 int dfn[maxn],low[maxn],dfs_clock;
8882 int st[maxn*2],top;bool ok[maxn];
5013 vector<int> ans;vector<int> temp;
4d9b int m,n;
453e inline void addEdge(int x,int y){
4704     tot++;des[tot] = y;
6d84     nxt[tot] = first[x];first[x] = tot;
95cf }
0e91 void input(){
9af0     cin>>n>>m;
356f     for (int i=0;i<m;i++){
17be         int u,v;scanf("%d%d",&u,&v);
ad4e         addEdge(u,v);addEdge(v,u);
95cf     }
95cf }
312b void dfs(int u,int fa){
d413     dfn[u] = low[u] = ++dfs_clock;
3ddf     for (int t = first[u];t;t=nxt[t]){
e8e0         int v = des[t];
b6ee         if (v==fa)continue;
3c64         if (!dfn[v]){
5248             st[top++] = t;dfs(v,u);
a19f             low[u] = min(low[u],low[v]);
9cb7             if (low[v]>=dfn[u]){
9d83                 bcc_cnt++;ok[bcc_cnt] = true;
1a7e                 temp.clear();
1026                 while (true){
87f2                     int tt = st[--top];
0648                     temp.push_back((tt+1)/2);
cf0f                     if (bcc_no[des[tt]]!=bcc_cnt){
aff7                         bcc_no[des[tt]] = bcc_cnt;
3e93                         cnt_n[bcc_cnt]++;
8e2e                     }else{
e551                         ok[bcc_cnt] = false;
95cf                     }
83bb                     cnt_e[bcc_cnt]++;
5047                     if (tt==t)break;
95cf                 }
b114                 if (ok[bcc_cnt]&&temp.size()>1){
af9b                     for (int i=0;i<temp.size();i++){
90d3                         ans.push_back(temp[i]);
95cf                     }
95cf                 }
95cf             }
e245         }else if (dfn[v]<dfn[u]){
be8d             st[top++] = t;
769a             low[u] = min(low[u],dfn[v]);
95cf         }
95cf     }
95cf }
```

```
9627 void solve(){
c2a0     for (int i=1;i<=n;i++){if (!dfn[i])dfs(i,-1);}
e139     sort(ans.begin(),ans.end());
c4d5     cout<<ans.size()<<endl;
263e     for (int i=0;i<ans.size();i++){printf("%d ",ans[i]);}
95cf }
3117 int main(){
2a5c     input();
ccd1     solve();
7021     return 0;
95cf }
```

5.3 Tarjan(SCC)

```
302f #include<bits/stdc++.h>
421c using namespace std;
52c1 const int maxn = 1e5+100;
04f1 int m,n,h;int t[maxn];
7560 int first[maxn*2],nxt[maxn*2],des[maxn*2],tot;
eaf3 int dfn[maxn],low[maxn],dft;bool d[maxn];
414b int flag[maxn],cnt[maxn],scc;stack<int> stk;
e50d bool in[maxn];
704e inline void add(int x,int y){
4704     tot++;des[tot] =y;
6d84     nxt[tot] = first[x];first[x] =tot;
95cf }
a4ef void tar(int node){
b081     dfn[node] = low[node] = ++dft;
5782     in[node] = 1;stk.push(node);
e83e     for (int t = first[node];t;t=nxt[t]){
e8e0         int v = des[t];
3c64         if (!dfn[v]){
53e9             tar(v);
9ee1             low[node] = min(low[node],low[v]);
8734         }else if (in[v]){
d1ad             low[node] = min(low[node],dfn[v]);
95cf         }
95cf     }
bb4b     if (dfn[node]==low[node]){
38ac         scc++;
1026         while (true){
6947             int temp = stk.top();
80c2             flag[temp]=scc;
5685             in[temp] = 0;
b820             cnt[scc]++;stk.pop();
ea28             if (temp==node)break;
95cf         }
95cf     }
95cf }
3117 int main(){
d994     scanf("%d%d%d",&n,&m,&h);
b8ca     for (int i=1;i<=n;i++){scanf("%d",t+i);}
356f     for (int i=0;i<m;i++){
4d1b         int u1,u2;scanf("%d%d",&u1,&u2);
7ec2         if (t[u1]==(t[u2]+1)%h)add(u2,u1);
e284         if (t[u2]==(t[u1]+1)%h)add(u1,u2);
95cf     }
6d72     for (int i=1;i<=n;i++){if (!dfn[i])tar(i);}
6dbf     for (int i=1;i<=n;i++){
f030         for (int t = first[i];t;t=nxt[t]){
f3e2             if (flag[i]==flag[des[t]])continue;
a099             else{d[flag[i]]++;}
95cf         }
95cf     }
61a1     cnt[0] =n+1;int ans = 0;
5176     for (int i=1;i<=scc;i++){
83aa         if (d[i]==0&&cnt[i]<cnt[ans]){ans = i;}
95cf     }
31ae     cout<<cnt[ans]<<endl;
6dbf     for (int i=1;i<=n;i++){
e341         if (flag[i]==ans){cout<<i<<" ";}
95cf     }
3251     cout<<endl;
7021     return 0;
95cf }
```

5.4 Dijkstra

```
427e // Created by calabash_boy on 18-11-13.
427e // remain k bi-edge such that the most points' dis == min_dis
302f #include <bits/stdc++.h>
421c using namespace std;
4085 typedef long long ll;
1c1d const ll inf_ll = 0x3f3f3f3f3f3f3f3fll;
```

```
a7c7 const int inf = 0x3f3f3f3f;
8856 const int maxn = 300005;
aaaa struct EDGE{int first,second,third;};
47a0 int n,m,k;
04e9 namespace Short_Path_Tree{
db9e     vector<pair<int,int> > Edge[maxn];
727f     bool used[maxn];
b200     void add_edge(int x,int y,int w) {Edge[x].push_back({y,w});}
1e0b     void output(const vector<int> &ans){
90f7         printf("%d\n",(int) ans.size());
69cb         for (int v : ans)printf("%d␣",v);
dcec         puts("");exit(0);
95cf     }
2fb6     void solve(int K){
8c27         vector<int> ans(0);queue<int> Q;
2ad2         used[1] = 1;Q.push(1);
11e5         while (!Q.empty()){
440f             if (ans.size()== K)output(ans);
ff8a             int head = Q.front();Q.pop();
79f8             for (auto pr : Edge[head]){
1ddf                 if (used[pr.first])continue;
5046                 used[pr.first] = 1;
fb50                 ans.push_back(pr.second);
b172                 Q.push(pr.first);
440f                 if (ans.size()==K)output(ans);
95cf             }
95cf         }
25fd         output(ans);
95cf     }
329b };
b049 namespace Dijkstra{
26a7     ll dis[maxn];bool used[maxn];
d92b     vector<EDGE > *Edge;int S,N;
80b8     struct Node{
386c         int x;ll dis;
647a         bool operator < (const Node &other)const{
717e             return other.dis < dis;
95cf         }
329b     };
4826     void init(vector<EDGE>*Edgee,int n,int st){
96ad         Edge = Edgee;S =st;N = n;
95cf     }
ec07     void work(){
2560         memset(dis,inf,sizeof dis);
c124         priority_queue<Node> pq;
b911         dis[S] = 0;pq.push({S,0});
57d6         while (!pq.empty()){
d5d6             Node head = pq.top();pq.pop();
7583             if (used[head.x])continue;
e4b5             used[head.x] = 1;
1a52             for (auto pr : Edge[head.x]){
2fbb                 if (dis[pr.first] > dis[head.x] + pr.second){
d59f                     dis[pr.first] = dis[head.x] + pr.second;
d53e                     pq.push({pr.first,dis[pr.first]});
95cf                 }
95cf             }
95cf         }
95cf     }
c844     void extract_spt(){
5cdb         for (int u=1;u<=N;u++){
79f0             for (auto pr : Edge[u]){
091e                 if (dis[pr.first] == dis[u] + pr.second){
e042                     Short_Path_Tree::add_edge(u,pr.first,pr.third);
95cf                 }
95cf             }
95cf         }
95cf     }
329b };
cae8 vector<EDGE> E[maxn];
3117 int main(){
7ffc     scanf("%d%d%d",&n,&m,&k);
e052     for (int i=1;i<=m;i++){
58ac         int x,y,w;scanf("%d%d%d",&x,&y,&w);
53d8         E[x].push_back({y,w,i});
fd97         E[y].push_back({x,w,i});
95cf     }
080d     Dijkstra::init(E,n,1);
f9c1     Dijkstra::work();
1170     Dijkstra::extract_spt();
734c     Short_Path_Tree::solve(k);
7021     return 0;
95cf }
```

5.5 Dijkstra interval graph

```
427e // CF 786B
```

```
302f #include<bits/stdc++.h>
421c using namespace std;
52c1 const int maxn = 1e5 + 100;
0c86 const int N = 10 * maxn;
4085 typedef long long ll;
b049 namespace Dijkstra{
3a06     vector<pair<int,int> > E[N];
e7eb     ll dis[N];
5269     bool used[N];
bb4b     inline void add_edge(int u,int v,int w){
88d1         E[u].push_back(make_pair(v,w));
95cf     }
9fbb     void dijkstra(int S, int N){
69f6         priority_queue<pair<ll,int> > pq;
cd0f         for (int i=1;i<=N;i++){
4d17             dis[i] = 0x3f3f3f3f3f3f3f3fll;
fc61             used[i] = 0;
95cf         }
4fb7         dis[S] = 0;
cd0f         for (int i=1;i<=N;i++){
0f64             pq.push(make_pair(-dis[i],i));
95cf         }
57d6         while (!pq.empty()){
63ef             pair<ll,int> head = pq.top();pq.pop();
c89e             int u; ll dist;
4067             tie(dist,u) = head;
c884             dist *= -1;
9a95             if (used[u])continue;
db27             used[u] = 1;
48e2             for (auto e : E[u]){
33b3                 int v,len;
ccc4                 tie(v,len) = e;
f6e6                 if (dis[v] > dist + len){
078a                     dis[v] = dist + len;
d06d                     pq.push(make_pair(-dis[v],v));
95cf                 }
95cf             }
95cf         }
95cf     }
756f     void output(int n){
6dbf         for (int i=1;i<=n;i++){
b158             printf("%lld ",dis[i] == 0x3f3f3f3f3f3f3f3fll ? -1:dis[i]);
95cf         }
885d         puts("");
95cf     }
}
24fc int n,q,s;
9f58 int cnt;
23cc struct SegmentTree{
c7e5     int id[maxn*4];
9476     void build(int x,int l,int r,bool up){
6281         id[x] = ++cnt;
3a0d         if (l == r){
c35b             int u = id[x];
d74c             int v = l;
2d00             if (up)swap(u,v);
a9ea             Dijkstra::add_edge(u, v, 0);
4f2d             return;
95cf         }
b8b7         int mid = l + r >> 1;
8094         build(x<<1,l,mid,up);
7d97         build(x<<1|1,mid+1,r,up);
c35b         int u = id[x];
dc32         int v = id[x<<1];
2d00         if (up)swap(u,v);
a9ea         Dijkstra::add_edge(u, v, 0);
a419         u = id[x];
e9c6         v = id[x<<1|1];
2d00         if (up)swap(u,v);
a9ea         Dijkstra::add_edge(u, v, 0);
95cf     }
3e8e     void add_edge(int x,int l,int r,int L,int R, int T, int w, bool up){
d499         if (l > R || L > r)return;
4d29         if (L <= l && r <= R){
c35b             int u = id[x];
8863             int v = T;
2d00             if (up)swap(u,v);
4c45             Dijkstra::add_edge(u, v, w);
4f2d             return;
95cf         }
b8b7         int mid = l + r >> 1;
9083         add_edge(x<<1, l, mid, L, R, T, w, up);
edd2         add_edge(x<<1|1, mid+1, r, L, R, T, w, up);
95cf     }
dfc9 }Down,Up;
3117 int main(){
13bb     scanf("%d%d%d",&n,&q,&s);
811f     cnt = n;
95cf     }
95cf }
24fc int n,q,s;
9f58 int cnt;
23cc struct SegmentTree{
c7e5     int id[maxn*4];
9476     void build(int x,int l,int r,bool up){
6281         id[x] = ++cnt;
3a0d         if (l == r){
c35b             int u = id[x];
d74c             int v = l;
2d00             if (up)swap(u,v);
a9ea             Dijkstra::add_edge(u, v, 0);
4f2d             return;
95cf         }
b8b7         int mid = l + r >> 1;
8094         build(x<<1,l,mid,up);
7d97         build(x<<1|1,mid+1,r,up);
c35b         int u = id[x];
dc32         int v = id[x<<1];
2d00         if (up)swap(u,v);
a9ea         Dijkstra::add_edge(u, v, 0);
a419         u = id[x];
e9c6         v = id[x<<1|1];
2d00         if (up)swap(u,v);
a9ea         Dijkstra::add_edge(u, v, 0);
95cf     }
3e8e     void add_edge(int x,int l,int r,int L,int R, int T, int w, bool up){
d499         if (l > R || L > r)return;
4d29         if (L <= l && r <= R){
c35b             int u = id[x];
8863             int v = T;
2d00             if (up)swap(u,v);
4c45             Dijkstra::add_edge(u, v, w);
4f2d             return;
95cf         }
b8b7         int mid = l + r >> 1;
9083         add_edge(x<<1, l, mid, L, R, T, w, up);
edd2         add_edge(x<<1|1, mid+1, r, L, R, T, w, up);
95cf     }
dfc9 }Down,Up;
3117 int main(){
13bb     scanf("%d%d%d",&n,&q,&s);
811f     cnt = n;
```

```
d237     Down.build(1, 1, n, false);
c1bc     Up.build(1, 1, n, true);
2cc8     while (q--){
aa14         int t,u,l,r,w;
8661         scanf("%d",&t);
8204         if (t == 1){
3b67             int v;
95a1             scanf("%d%d%d",&u,&v, &w);
8637             l = r = v;
96c0             t = 2;
8e2e         }else{
168f             scanf("%d%d%d%d",&u,&l,&r,&w);
95cf         }
163d         if (t == 2){
427e             // u -> [l,r], len = w
63b8             Down.add_edge(1, 1, n, l, r, u, w, true);
8e2e         }else{
427e             // [l,r] -> v, len = w
c4a7             Up.add_edge(1, 1, n, l, r, u, w, false);
95cf         }
95cf     }
3fd3     Dijkstra::dijkstra(s, cnt);
d041     Dijkstra::output(n);
7021     return 0;
95cf }
```

5.6 Eulor Tour

```
302f #include<bits/stdc++.h>
421c using namespace std;
52c1 const int maxn = 1e5 + 100;
a71b const int maxm = 5e5 + 100;
35b8 int n,m;
03f0 int d[maxn];
427e //<点，到这个点走的边id>
c49a vector<pair<int,int> > tour;
37e9 vector<pair<int,int> > E[maxn];
052c pair<int,int> edge[maxm];
f231 bool used[maxm];
880a int now[maxn];
5331 void dfs(int u,int e_id){
18c2     for (; now[u] < E[u].size(); now[u] ++){
6003         int v,id;
c7a3         tie(v,id) = E[u][now[u]];
1e6c         if (used[id]) continue;
6be5         used[id] = 1;
038b         dfs(v,id);
95cf     }
4556     tour.push_back(make_pair(u,e_id));
95cf }
3117 int main(){
ac98     scanf("%d%d",&n,&m);
e052     for (int i=1;i<=m;i++){
e635         int a,b;
a6b8         scanf("%d%d",&a,&b);
4a7b         edge[i] = make_pair(a,b);
7462         E[a].push_back(make_pair(b,i));
2a96         E[b].push_back(make_pair(a,i));
95cf     }
4e9d     dfs(1,-1);
8d42     reverse(tour.begin(), tour.end());
87e7     /*
3977      for (auto pr : tour){
6b5b      int u,id;
2e37      tie(u,id) = pr;
6b68      cerr<<u<<" "<<id<<endl;
95cf      }
f2b5      */
7021     return 0;
95cf }
```

6 Graph/Tree

6.1 Divide & Conquer of Point

```
427e //
427e // Created by calabash_boy on 18-10-6.
427e //
427e //求树上长度小于等于k的有向路径数
1915 #include<stdio.h>
54ff #include<algorithm>
ef2f #include<cstring>
421c using namespace std;
bbaa const int MAX = 1e4+100;
```

```
08a4 const int INF = 0x3f3f3f3f;
0b89 int first [MAX*2]; int des[MAX*2];
3efe int len[MAX*2]; int nxt[MAX*2];
956f int n,k,tot; int a[MAX]; int sum[MAX];
ecb3 int dp[MAX]; int dis[MAX]; int num,ans;
aa8d bool vis[MAX]; int Sum,Min,Minid;
5d53 void init(){
57d5     memset(first,0,sizeof first);
7ae1     tot =0; ans =0;
87fb     memset(vis,0,sizeof vis);
95cf }
ce82 inline void add(int x,int y,int z){
71cf     tot++;
3615     des[tot]= y; len[tot] =z;
6d84     nxt[tot] = first[x]; first[x] = tot;
95cf }
0e91 void input(){
324a     for (int i=1;i<n;i++){
3676         int u,v,w;
95a1         scanf("%d%d%d",&u,&v,&w);
43a8         add(u,v,w); add(v,u,w);
95cf     }
95cf }
da46 void dfs1(int node,int father){
90d3     sum[node] = 1; dp[node] = 0;
e83e     for (int t = first[node];t;t = nxt[t]){
e8e0         int v = des[t];
c80a         if (v == father||vis[v]){
b333             continue;
95cf         }
d58d         dfs1(v,node);
cb59         sum[node] += sum[v];
2cf9         dp[node] = max(dp[node],sum[v]);
95cf     }
95cf }
2d8d void dfs2(int node,int father){
4ab1     int temp = max(dp[node],Sum-sum[node]);
d6e3     if (temp<Min){
76f6         Min = temp; Minid = node;
95cf     }
e83e     for (int t = first[node];t;t = nxt[t]){
e8e0         int v = des[t];
a37f         if (v==father||vis[v]){ continue; }
253c         dfs2(v,node);
95cf     }
95cf }
6fae int getRoot(int u){
8e67     dfs1(u,0); Sum = sum[u];
3069     Min = INF; Minid = -1;
005f     dfs2(u,0);
1090     return Minid;
95cf }
4ac1 void getDist(int node,int father,int dist){
e097     dis[num++] = dist;
e83e     for (int t = first[node];t;t = nxt[t]){
e8e0         int v =des[t];
a37f         if (v == father||vis[v]){ continue; }
6cae         getDist(v,node,dist+len[t]);
95cf     }
95cf }
97e3 int calc (int u,int val){
9daa     num=0; int res =0;
d05a     getDist(u,0,0);
4b02     sort(dis,dis+num);
e78d     int i=0;int j=num-1;
6f80     while (i<j){
e6c0         if (dis[i]+dis[j]+2*val<=k){
efef             res+=j-i;
a42b             i++;
5cd2         }else{ j--; }
95cf     }
244d     return res;
95cf }
ee28 void solve(int u){
b583     int root = getRoot(u);
b2e3     ans +=calc(root,0); vis[root] = true;
235c     for (int t = first[root];t;t = nxt[t]){
e8e0         int v = des[t];
332f         if (vis[v]){
b333             continue;
95cf         }
91fa         ans-=calc(v,len[t]);
a707         solve(v);
95cf     }
95cf }
3117 int main(){
7666     while (scanf("%d%d",&n,&k)!=EOF&&n&&k){
07e2         init();
```

```
2a5c         input();
1d60         solve(1);
53b1         printf("%d\n",ans);
95cf     }
7021     return 0;
95cf }
```

6.2 Divide & Conquer of Edge

```
427e // Created by calabash_boy on 2019/10/15.
427e // Luogu 5115.SAM + 边分 + 虚树DP: Given S, calculate
427e // \sum_{i<j and LCP(i,j)<=K1 and LCS(i,j)<=K2}{LCS(i,j) * LCP(i,j)}
427e // 最大度数有限制（例如parent树27度），则不需要三度化。
302f #include<bits/stdc++.h>
421c using namespace std;
eb45 const int maxn = 2e5 + 100;
b1f7 char s[maxn],t[maxn];int n,K1,K2;
3e3e struct Suffix_Automaton{
0037     int nxt[maxn*2][26],fa[maxn*2],l[maxn*2];
0db0     int last,cnt;
c75a     Suffix_Automaton(){ clear(); }
1126     void clear(){
8bdb         last =cnt=1;fa[1]=l[1]=0;
9b85         memset(nxt[1],0,sizeof nxt[1]);
95cf     }
e798     void init(char *s){
0bef         while (*s){add(*s-'a');s++;}
95cf     }
681b     void add(int c){
ee06         int p = last, np = ++cnt;
8b9f         memset(nxt[cnt],0,sizeof nxt[cnt]);
97c0         l[np] = l[p]+1;last = np;
b7f5         while (p&&!nxt[p][c])nxt[p][c] = np,p = fa[p];
fdc4         if (!p)fa[np]=1;
037f         else{
5740             int q = nxt[p][c];
d84d             if (l[q]==l[p]+1)fa[np] =q;
037f             else{
2401                 int nq = ++ cnt;
bc67                 l[nq] = l[p]+1;
da26                 memcpy(nxt[nq],nxt[q],sizeof (nxt[q]));
66a6                 fa[nq] =fa[q];fa[np] = fa[q] =nq;
5dc1                 while (nxt[p][c]==q)nxt[p][c] =nq,p = fa[p];
95cf             }
95cf         }
95cf     }
0d52     void extract(vector<int> * E,char *s,int n,int *id,int *dep,int K){
3c9b         int temp = 1;
1294         for (int i=0;i<n;i++){
ac16             temp = nxt[temp][s[i] - 'a'];
7eb8             id[temp] = i + 1;
95cf         }
e3bd         for (int i=2;i<=cnt;i++)E[fa[i]].push_back(i);
7b35         for (int i=1;i<=cnt;i++){
9a67             if (l[i] <= K)dep[i] = l[i];
4cb5             else dep[i] = 0;
95cf         }
95cf     }
0fd0 }sam1,sam2;
9ac5 vector<int> EE1[maxn * 2],E2[maxn*2];
90b0 vector<tuple<int,int,int> > E1[maxn*4];
9ea3 int idd1[maxn * 2],id1[maxn*4];
885f int depp1[maxn * 2],dep1[maxn*4];
0fbb int id2[maxn* 2],dep2[maxn*2];
223d bool can_use[maxn*4];
8adf int edge_cnt = 0;
4e0e int cnt, st[maxn * 2][20], depth[maxn * 2];
a210 int pos2[maxn*2],pos1[maxn*4];
9156 int dfs_clock,l[maxn*2],r[maxn*2];
c2d4 void dfs2(int u,int fa){
bf7e     l[u] = ++dfs_clock;
98f1     st[u][0] = fa;
8ec8     depth[u] = depth[fa] + 1;
c19b     for (int i=1;i<20 && st[u][i-1];i++){
df83         st[u][i] = st[st[u][i-1]][i-1];
95cf     }
8622     for (auto v : E2[u]){
b6ee         if (v == fa)continue;
3e76         dfs2(v,u);
95cf     }
f142     r[u] = dfs_clock;
95cf }
7ed5 int get_lca(int u,int v){
08ee     if (depth[u] < depth[v])swap(u,v);
1534     for (int i=19;i>=0;i--){
f2cc         if (depth[st[u][i]] >= depth[v])u = st[u][i];
```

```
95cf     }
c698     if (u == v)return u;
1534     for (int i=19;i>=0;i--){
8ce3         if (st[u][i] != st[v][i]){
aaf6             u = st[u][i];v = st[v][i];
95cf         }
95cf     }
178b     assert(st[u][0] == st[v][0]);
d6f1     return st[u][0];
95cf }
427e //三度化
7d3c int dfs(int u,int fa){
72bd     int now = ++cnt;
63f2     id1[now] = idd1[u];dep1[now] = depp1[u];
8d7f     pos1[id1[now]] = now;
b669     int pre = now;
f4be     for (auto v : EE1[u]){
b6ee         if (v == fa)continue;
71b8         int temp = ++cnt;
72ac         id1[temp] = 0;dep1[temp] = depp1[u];
d721         edge_cnt ++;
d805         E1[pre].push_back(make_tuple(temp,dep1[temp] - dep1[pre],edge_cnt));
4478         E1[temp].push_back(make_tuple(pre,dep1[temp] - dep1[pre],edge_cnt));
1b1e         int vid = dfs(v,u);
d721         edge_cnt ++;
696d         E1[temp].push_back(make_tuple(vid,dep1[vid] - dep1[temp],edge_cnt));
e45d         E1[vid].push_back(make_tuple(temp,dep1[vid] - dep1[temp],edge_cnt));
8dde         pre = temp;
95cf     }
7d47     return now;
95cf }
889f long long ans = 0;
fbd5 int sz[maxn*4];
bc69 int dis[maxn* 4];
8db0 void dfs_dis(int u,int fa,int len){
ac19     dis[u] = len;
6eaa     for (auto e : E1[u]){
7d8f         int v,lll,edge_id;tie(v,lll,edge_id) = e;
20c6         if (v == fa || !can_use[edge_id])continue;
03ed         dfs_dis(v,u,len + lll);
95cf     }
95cf }
3183 void dfs_sz(int u,int fa){
50c0     sz[u] = 1;
6eaa     for (auto e : E1[u]){
5d3a         int v,len,edge_id;tie(v,len,edge_id) = e;
20c6         if (v == fa || !can_use[edge_id])continue;
4934         dfs_sz(v,u);
8449         sz[u] += sz[v];
95cf     }
95cf }
af5f void dfs_edge(int u,int fa,int &e_id,int &uu,int &vv,int &ww,int &max_sz,int
       tot_node){
6eaa     for (auto e : E1[u]){
5d3a         int v,len,edge_id;tie(v,len,edge_id) = e;
20c6         if (v == fa || !can_use[edge_id])continue;
5841         int max_sz_t = max(sz[v],tot_node - sz[v]);
6b23         if (max_sz_t < max_sz){
4d92             max_sz = max_sz_t;
8a53             uu = u;vv = v;ww = len;e_id = edge_id;
95cf         }
6498         dfs_edge(v,u,e_id,uu,vv,ww,max_sz,tot_node);
95cf     }
95cf }
11d5 void dfs_node(int u,int fa,vector<int> &nodes){
d7fa     if (id1[u])nodes.push_back(id1[u]);
6eaa     for (auto e : E1[u]){
5d3a         int v,len,edge_id;tie(v,len,edge_id) = e;
20c6         if (v == fa || !can_use[edge_id])continue;
2f72         dfs_node(v,u,nodes);
95cf     }
95cf }
31b7 int color[maxn * 2];
d862 int vis[maxn];
d6e7 long long dp[maxn * 2];
1207 long long dp_cnt[maxn*2][2];
2ec5 long long dp_sum[maxn*2][2];
cafd int stk[maxn*2];
3abd int fa[maxn*2];
8345 inline void clear(int x,int type){
e238     dp[x] = 0;vis[x] = type;
a8b8     for (int c = 0; c < 2;c ++)dp_cnt[x][c] = dp_sum[x][c] = 0;
95cf }
74bd void DP(vector<int> & nodes_,int ww){
1112     vector<int> nodes(0);
00c4     for (int x : nodes_){
0d7f         nodes.push_back(pos2[x]);
95cf     }
```

```
4619    for (int x : nodes)clear(x,1);
d5d4    sort(nodes.begin(),nodes.end(),[](int x,int y){
c861        return l[x] < l[y];
b251    });
98e5    int SZ = nodes.size();
8d5c    for (int i=1;i<SZ;i ++){
0378        int temp = get_lca(nodes[i-1],nodes[i]);
ada3        if (!vis[temp]){
f11a            nodes.push_back(temp);
9df9            clear(temp,2);
95cf        }
95cf    }
5557    if (!vis[1]){
1428        nodes.push_back(1);
74de        clear(1,2);
95cf    }
d5d4    sort(nodes.begin(),nodes.end(),[](int x,int y){
c861        return l[x] < l[y];
b251    });
323d    int top = 1;
2894    stk[0] = nodes[0];
031f    for (int i=1;i<nodes.size();i++){
8825        while (l[nodes[i]] > r[stk[top-1]]) top --;
cf1f        fa[nodes[i]] = stk[top-1];
67ba        stk[top++] = nodes[i];
95cf    }
8235    long long anss = 0;
ceb1    for (int i= nodes.size() - 1;i >=0 ;i --){
529a        int u = nodes[i], c = vis[u] == 1? color[id2[u]] - 1: -1;
c997        if (c != -1){
c4fa            long long A = dep1[pos1[id2[u]]] - dis[pos1[id2[u]]];
dbda            dp[u] += A * dp_cnt[u][!c] + dp_sum[u][!c];
18b4            dp[u] -= dp_cnt[u][!c] * ww;
b801            dp_cnt[u][c] ++;
e09a            dp_sum[u][c] += A;
95cf        }
405e        long long temp_ans = dp[u] * dep2[u];
81b7        assert(temp_ans %2 == 0);
516a        anss += temp_ans/2;
d9a7        dp[fa[u]] += dp_cnt[fa[u]][0] * dp_sum[u][1] + dp_cnt[u][0] * dp_sum[fa[
              u]][1];
041d        dp[fa[u]] += dp_cnt[fa[u]][1] * dp_sum[u][0] + dp_cnt[u][1] * dp_sum[fa[
              u]][0];
c5a9        dp[fa[u]] -= (dp_cnt[fa[u]][1] * dp_cnt[u][0] + dp_cnt[fa[u]][0] *
              dp_cnt[u][1]) * ww;
            for (int c = 0;c < 2;c ++){                                          4545
                dp_cnt[fa[u]][c] += dp_cnt[u][c];                                96b5
                dp_sum[fa[u]][c] += dp_sum[u][c];                                4009
            }                                                                    95cf
        }                                                                        95cf
        ans += anss;                                                             b484
        for (int x : nodes)vis[x] = 0;                                           70c2
    }                                                                            95cf
    void calc(int uu,int vv,int ww){                                             29be
        vector<int> L(0),R(0),nodes(0);                                          52e9
        dfs_node(uu,0,L);dfs_node(vv,0,R);                                       b258
        for (int x : L){color[x] = 1;nodes.push_back(x);}                        e503
        for (int x : R){color[x] = 2;nodes.push_back(x);}                        4e8a
        DP(nodes,ww);                                                            e5e6
    }                                                                            95cf
    void dfs(int root){                                                          35ab
        dfs_sz(root,0);                                                          f054
        int tot_node = sz[root];                                                 bfcc
        if (tot_node == 1)return;                                                11c5
        int edge_id,uu,vv,ww,max_sz = tot_node + 1;                              18a2
        dfs_edge(root,0,edge_id,uu,vv,ww,max_sz,tot_node);                       232d
        can_use[edge_id] = false;                                                5cf1
        dfs_dis(uu,0,0);dfs_dis(vv,0,0);                                         7e85
        calc(uu,vv,ww);dfs(uu);dfs(vv);                                          ab13
    }                                                                            95cf
    int main(){                                                                  3117
        scanf("%s%d%d",s,&K1,&K2);                                               c11b
        n = strlen(s);                                                           5264
        memcpy(t,s,sizeof s);reverse(t,t + n);                                   5f03
        sam1.init(s);sam2.init(t);                                               7dbf
        sam1.extract(EE1,s,n,idd1,depp1,K2);                                     b1ed
        sam2.extract(E2,t,n,id2,dep2,K1);                                        8ada
        for (int i=1;i<= sam2.cnt; i ++){                                        073d
            if (id2[i]){                                                         4ce1
                id2[i] = n + 1 - id2[i];                                         4913
                pos2[id2[i]] = i;                                                97e0
            }                                                                    95cf
        }                                                                        95cf
        int root1 = dfs(1,0);int root2 = 1;                                      b333
        dfs2(root2,0);                                                           ac7c
        memset(can_use,true,sizeof can_use);                                     fbab
        dfs(root1);                                                              4267
        cout<<ans<<endl;                                                         d592
```

```
7021     return 0;
95cf }
```

6.3 Heavy Light Decomposition

```
427e // Created by calabash_boy on 18-7-3.
427e //统计路径上标记边的个数
302f #include<bits/stdc++.h>
421c using namespace std;
8e62 const int maxn = 500000+100;
4bc9 int n,q,m,Root;  char s[10];
5f7d struct BIT{
3bf5     int sm[maxn];
cf5a     int lowbit(int _x){return _x&(-_x);}
d5af     void build (int l,int r){
5023         for (int i=l;i<=r;i++)add(i,1);
95cf     }
6142     void add(int x,int val){
dc9a         while (x<=maxn){
9ccc             sm[x]+=val;x+=lowbit(x);
95cf         }
95cf     }
eb61     int sum(int x){
5839         int res =0;
6f1c         while (x){
e64f             res+=sm[x];
e6b6             x-=lowbit(x);
95cf         }
244d         return res;
95cf     }
9fc7     int query_sum(int l,int r){
7789         return sum(r)-sum(l-1);
95cf     }
b0c1 }tree;
9c21 namespace Heavy_Light_Decomposition{
7b14     int first[maxn*2];int nxt[maxn*2];int des[maxn*2];
cd30     int tot,cnt=0;
0d93     int tpos[maxn];int dep[maxn];int top[maxn];
d6bf     int fa[maxn]; int wson[maxn];  int sz[maxn];
f9d3     inline void addEdge(int _u, int _v){
26b9         des[++tot] = _v;
a66a         nxt[tot] = first[_u];
593b         first[_u] = tot;
95cf     }
427e     //统计dep，子树sz，重儿子wson
dd7c     void dfs(int node,int father){
c5b1         dep[node] = dep[father]+1;
afa3         fa[node] = father;  sz[node] =1;
e83e         for (int t = first[node];t;t = nxt[t]){
e8e0             int v = des[t];
e092             if (v==father){  continue;  }
1f8e             dfs(v,node);
acb3             if (sz[v]>sz[wson[node]]){
44c0                 wson[node] = v;
95cf             }
47d5             sz[node]+=sz[v];
95cf         }
95cf     }
427e     //node所在链的头是chain
aee5     void dfs2(int node,int father,int chain){
950f         top[node] = chain;  tpos[node] = ++cnt;
d010         if (wson[node]){
0f73             dfs2(wson[node],node,chain);
95cf         }
e83e         for (int t = first[node];t;t = nxt[t]){
e8e0             int v = des[t];
b928             if (v==father||v ==wson[node]){  continue;  }
e6aa             dfs2(v,node,v);
95cf         }
95cf     }
c352     /* s 树根 */
1a86     void init(int root){
5136         dfs(root,0);
7cdf         dfs2(root, 0, root);
95cf     }
620b     int lca(int x,int y){
d2f8         while (top[x]!=top[y]){
0cc5             if (dep[top[x]]<dep[top[y]]){swap(x,y);}
7456             x = fa[top[x]];
95cf         }
d22b         if (dep[x]<dep[y])swap(x,y);
c218         return y;
95cf     }
29cf     void modify(int u,int v){
733e         if (fa[u]!=v){  swap(u,v);  }
1e27         tree.add(tpos[u],-1);
```

```
95cf     }
1dc2     int get_sum(int u,int v){
5839         int res =0;
03a1         while (top[u]!=top[v]){
a716             if (dep[top[u]]<dep[top[v]]){  swap(u,v);  }
f1e8             res+= tree.query_sum(tpos[top[u]],tpos[u]);
005b             u = fa[top[u]];
95cf         }
4b1a         if (dep[u]<dep[v]){  swap(u,v); }
cbff         res += tree.query_sum(tpos[v],tpos[u]);
244d         return res;
95cf     }
95cf }
3117 int main(){
cd91     scanf("%d",&n);
324a     for (int i=1;i<n;i++){
17be         int u,v;  scanf("%d%d",&u,&v);
1478         Heavy_Light_Decomposition::addEdge(u, v);
e4e6         Heavy_Light_Decomposition::addEdge(v, u);
95cf     }
90e1     Heavy_Light_Decomposition::init(1);
427e     //维护
1ca5     tree.build(2,n);
ea85     scanf("%d",&q);
3605     q+=n-1;
2cc8     while (q--){
587c         scanf("%s",s);
5d10         if (s[0]=='W'){
3c9e             int x;
ea4e             scanf("%d",&x);
3b50             printf("%d\n",Heavy_Light_Decomposition::get_sum(1,x));
8e2e         }else{
0f8b             int x,y;
a9b3             scanf("%d%d",&x,&y);
a309             Heavy_Light_Decomposition::modify(x,y);
95cf         }
95cf     }
7021     return 0;
95cf }
```

6.4 Virtual Tree

```
//                                                                                  427e
// Created by calabash_boy on 18-10-6.                                             427e
//                                                                                  427e
                                                                                    427e
#include <bits/stdc++.h>                                                            302f
using namespace std;                                                                421c
typedef long long LL;                                                               5cad
const int maxn = 25e4+100;                                                          40fb
const LL INF = 0x3f3f3f3f3f3f3f3fLL;                                                b1ec
int first[maxn],des[maxn*2],nxt[maxn*2],tot;                                        58a9
int n,m;                                                                            35b8
LL dp[maxn],leng[maxn*2], len[maxn];                                                667a
int vis[maxn],dep[maxn],fa[maxn];                                                   e55b
int sz[maxn],wson[maxn],ttop[maxn],tfa[maxn];int k,h[maxn];                         21fe
int stk[maxn],top;int l[maxn],r[maxn],dfs_clock;                                    0a19
inline void addEdge(int x,int y,int w){                                             a50a
    tot++;                                                                          71cf
    des[tot] = y;leng[tot] = w;                                                     a752
    nxt[tot] = first[x];first[x] = tot;                                             6d84
}                                                                                   95cf
void dfs(int u,int fath){                                                           827d
    l[u] = ++dfs_clock;sz[u]=1;                                                     84cf
    for (int t = first[u];t;t=nxt[t]){                                              3ddf
        int v = des[t];                                                             e8e0
        if (v==fath)continue;                                                       9d74
        LL w = leng[t];                                                             62a8
        dep[v] = dep[u] + 1;tfa[v]=u;                                               e4a6
        len[v] = min(len[u],w);                                                     818a
        dfs(v,u);sz[u]+=sz[v];                                                      7457
        if (sz[v]>sz[wson[u]]){wson[u] = v;}                                        c7eb
    }                                                                               95cf
    r[u]=dfs_clock ;                                                                f142
}                                                                                   95cf
void dfs2(int u,int chain){                                                         4707
    ttop[u]=chain;                                                                  0865
    if (wson[u])dfs2(wson[u],chain);                                                d6b4
    for (int t = first[u];t;t=nxt[t]){                                              3ddf
        int v = des[t];                                                             e8e0
        if (v==tfa[u]||v==wson[u])continue;                                         0c51
        dfs2(v,v);                                                                  8064
    }                                                                               95cf
}                                                                                   95cf
int lca(int x,int y){                                                               620b
    while (ttop[x]!=ttop[y]){                                                       00da
```

```
6d86         if (dep[ttop[x]]<dep[ttop[y]])swap(x,y);
2df6         x = tfa[ttop[x]];
95cf     }
d22b     if (dep[x]<dep[y])swap(x,y);
c218     return y;
95cf }
4ac9 bool cmp(int x,int y){return l[x]<l[y];}
9627 void solve(){
c93a     scanf("%d",&k);
f3ea     for (int i=0;i<k;i++){
3596         scanf("%d",h+i);
a234         vis[h[i]]=1;dp[h[i]]=0;
95cf     }
f5bb     sort(h,h+k,cmp);
a555     int kk =k;
c701     for (int i=1;i<kk;i++){
4680         int temp = lca(h[i-1],h[i]);
b925         if (!vis[temp])vis[temp]=2,h[k++] =temp,dp[temp]=0;
95cf     }
22a9     if (!vis[1])vis[1]=2,h[k++]=1,dp[1]=0;
f5bb     sort(h,h+k,cmp);
25a6     top=1;stk[0]=h[0];
3ef4     for (int i=1;i<k;i++){
b35a         while (l[h[i]]>r[stk[top-1]])top--;
f930         fa[h[i]] = stk[top-1];
274e         stk[top++] =h[i];
95cf     }
5c52     for (int i=k-1;i>=0;i--){
dca2         if (vis[h[i]]==2)dp[h[i]] = min(dp[h[i]],len[h[i]]);
6a6b         else dp[h[i]] = len[h[i]];
d6ae         dp[fa[h[i]]]+=dp[h[i]];
95cf     }
c682     printf("%lld\n",dp[1]);
f3ea     for (int i=0;i<k;i++){
e3ec         vis[h[i]]=0;
95cf     }
95cf }
3117 int main(){
cd91     scanf("%d",&n);
324a     for (int i=1;i<n;i++){
3676         int u,v,w;
95a1         scanf("%d%d%d",&u,&v,&w);
8796         addEdge(u,v,w);addEdge(v,u,w);
95cf     }
8694     len[0] = len[1] = INF;
0e9e     dfs(1,-1);dfs2(1,1);
aa8d     scanf("%d",&m);
74ed     while (m--){solve();}
7021     return 0;
95cf }
```

7 Math

7.1 FFT

```
427e // Created by calabash_boy on 18-6-18.
302f #include <bits/stdc++.h>
421c using namespace std;
e48c namespace fft {
427e     //attention data type
53f7     typedef long long type;
f7dc     typedef double db;
e718     struct cp {
ba04         db x, y;
cfb3         cp() { x = y = 0; }
f329         cp(db x, db y) : x(x), y(y) {}
329b     };
9f2f     cp operator+(cp a, cp b) { return cp(a.x + b.x, a.y + b.y); }
624b     cp operator-(cp a, cp b) { return cp(a.x - b.x, a.y - b.y); }
36fe     cp operator*(cp a, cp b) { return cp(a.x * b.x - a.y * b.y, a.x * b.y + a.y
           * b.x); }
a0e1     cp conj(cp a) { return cp(a.x, -a.y); }
6ecb     type base = 1;
44b9     vector<cp> roots = {{0, 0}, {1, 0}};
3a50     vector<type> rev = {0, 1};
3f9e     const db PI = acosl(-1.0);
2b5b     void ensure_base(type nbase) {
7037         if (nbase <= base) return;
bbb1         rev.resize(static_cast<unsigned long>(1 << nbase));
89c3         for (type i = 0; i < (1 << nbase); i++) {
33a9             rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (nbase - 1));
95cf         }
a0ef         roots.resize(static_cast<unsigned long>(1 << nbase));
7acf         while (base < nbase) {
cd10             db angle = 2 * PI / (1 << (base + 1));
f864             for (type i = 1 << (base - 1); i < (1 << base); i++) {
```

```
b824                roots[i << 1] = roots[i];
90ee                db angle_i = angle * (2 * i + 1 - (1 << base));
a5d7                roots[(i << 1) + 1] = cp(cos(angle_i), sin(angle_i));
95cf            }
d27a            base++;
95cf        }
95cf    }
3548    void fft(vector<cp> &a, type n = -1) {
805a        if (n == -1) n = a.size();
2fa3        assert((n & (n - 1)) == 0);
dca5        type zeros = __builtin_ctz(n);
c44f        ensure_base(zeros);
a1b9        type shift = base - zeros;
800c        for (type i = 0; i < n; i++) {
aa3c            if (i < (rev[i] >> shift)) {
669c                swap(a[i], a[rev[i] >> shift]);
95cf            }
95cf        }
5911        for (type k = 1; k < n; k <<= 1) {
b660            for (type i = 0; i < n; i += 2 * k) {
b247                for (type j = 0; j < k; j++) {
7dca                    cp z = a[i + j + k] * roots[j + k];
ee2d                    a[i + j + k] = a[i + j] - z;
4da7                    a[i + j] = a[i + j] + z;
95cf                }
95cf            }
95cf        }
95cf    }
fbc2    vector<cp> fa, fb;
6833    vector<type> multiply(vector<type> &a, vector<type> &b) {
02f0        type need = a.size() + b.size() - 1;
cf09        type nbase = 0;
0c88        while ((1 << nbase) < need) nbase++;
6f7d        ensure_base(nbase);
cb07        type sz = 1 << nbase;
b44d        if (sz > (type) fa.size())
74d8            fa.resize(static_cast<unsigned long>(sz));
46e8        for (type i = 0; i < sz; i++) {
2155            type x = (i < (type) a.size() ? a[i] : 0);
f2d7            type y = (i < (type) b.size() ? b[i] : 0);
140d            fa[i] = cp(x, y);
95cf        }
eb13        fft(fa, sz);
53b1        cp r(0, -0.25 / sz);
6611        for (type i = 0; i <= (sz >> 1); i++) {
3695            type j = (sz - i) & (sz - 1);
f17e            cp z = (fa[j] * fa[j] - conj(fa[i] * fa[i])) * r;
4a23            if (i != j) {
0628                fa[j] = (fa[i] * fa[i] - conj(fa[j] * fa[j])) * r;
95cf            }
8cd4            fa[i] = z;
95cf        }
eb13        fft(fa, sz);
a834        vector<type> res(static_cast<unsigned long>(need));
4516        for (type i = 0; i < need; i++) {
1653            res[i] = fa[i].x + 0.5;
95cf        }
244d        return res;
95cf    }
3ca7    vector<type> multiply_mod(vector<type> &a, vector<type> &b, type m, type eq
          = 0) {
02f0        type need = a.size() + b.size() - 1;
cf09        type nbase = 0;
0c88        while ((1 << nbase) < need) nbase++;
6f7d        ensure_base(nbase);
cb07        type sz = 1 << nbase;
3292        if (sz > (type) fa.size()) {
74d8            fa.resize(static_cast<unsigned long>(sz));
95cf        }
2f67        for (type i = 0; i < (type) a.size(); i++) {
cfe6            type x = (a[i] % m + m) % m;
7cb0            fa[i] = cp(x & ((1 << 15) - 1), x >> 15);
95cf        }
b1cb        fill(fa.begin() + a.size(), fa.begin() + sz, cp {0, 0});
eb13        fft(fa, sz);
8c71        if (sz > (type) fb.size()) {
14b9            fb.resize(static_cast<unsigned long>(sz));
95cf        }
2cba        if (eq) {
88c2            copy(fa.begin(), fa.begin() + sz, fb.begin());
8e2e        } else {
0ac2            for (type i = 0; i < (type) b.size(); i++) {
ad83                type x = (b[i] % m + m) % m;
97f9                fb[i] = cp(x & ((1 << 15) - 1), x >> 15);
95cf            }
5f8e            fill(fb.begin() + b.size(), fb.begin() + sz, cp {0, 0});
e06b            fft(fb, sz);
95cf        }
```

```
d8f2        db ratio = 0.25 / sz;
9cc7        cp r2(0, -1);cp r3(ratio, 0);
0367        cp r4(0, -ratio);cp r5(0, 1);
6611        for (type i = 0; i <= (sz >> 1); i++) {
3695            type j = (sz - i) & (sz - 1);
996e            cp a1 = (fa[i] + conj(fa[j]));
a37e            cp a2 = (fa[i] - conj(fa[j])) * r2;
51fd            cp b1 = (fb[i] + conj(fb[j])) * r3;
ad90            cp b2 = (fb[i] - conj(fb[j])) * r4;
4a23            if (i != j) {
792b                cp c1 = (fa[j] + conj(fa[i]));
ecde                cp c2 = (fa[j] - conj(fa[i])) * r2;
18a0                cp d1 = (fb[j] + conj(fb[i])) * r3;
6ced                cp d2 = (fb[j] - conj(fb[i])) * r4;
28c4                fa[i] = c1 * d1 + c2 * d2 * r5;
178d                fb[i] = c1 * d2 + c2 * d1;
95cf            }
1184            fa[j] = a1 * b1 + a2 * b2 * r5;
87e9            fb[j] = a1 * b2 + a2 * b1;
95cf        }
922b        fft(fa, sz);fft(fb, sz);
a834        vector<type> res(static_cast<unsigned long>(need));
4516        for (type i = 0; i < need; i++) {
9dbc            long long aa = fa[i].x + 0.5;
d335            long long bb = fb[i].x + 0.5;
de5d            long long cc = fa[i].y + 0.5;
67e4            res[i] = (aa + ((bb % m) << 15) + ((cc % m) << 30)) % m;
95cf        }
244d        return res;
95cf    }
2307    vector<type> square_mod(vector<type> &a, type m) {
b845        return multiply_mod(a, a, m, 1);
95cf    }
329b };
eb45 const int maxn = 2e5+100;
86d1 int n,x;
7608 int a[maxn],sum[maxn],cnt[maxn];
a6aa vector<long long > A,B,C;
427e //example:
427e //f[i] = number of subsequences whose occurence of 1 is i.
427e //f[i] = \sum_{cnt[j]*cnt[j-i]}
3117 int main(){
a5fe    scanf("%d%d",&n,&x);cnt[0]=1;
6dbf    for (int i=1;i<=n;i++){
60cb        scanf("%d",a+i);
9a8f        sum[i] =sum[i-1];
1229        if(a[i]<x)sum[i]++;
6210        cnt[sum[i]]++;
95cf    }
bb11    A.resize(n*2+2);B.resize(n*2+2);
0423    for (int i=0;i<=n;i++){
1451        A[n+i] = cnt[i];B[n-i] = cnt[i];
95cf    }
284a    C = fft::multiply(A,B);
7cf7    C[n*2]-=n+1;C[n*2]>>=1;
d7c0    for (int i=n*2;i<=n*3;i++){ cout<<C[i]<<"␣"; }
7021    return 0;
95cf }
```

7.2 FWT

```
427e // Created by calabash_boy on 18-8-17.
427e //UOJ 310
302f #include<bits/stdc++.h>
421c using namespace std;
5cad typedef long long LL;
a923 const int N = 1048576;;
5bf2 const int MOD = 998244353;
2003 const int INV2 = (MOD+1)>>1;
4d4d const int INV4 = 1LL*INV2*INV2%MOD;
ac9d int a[N];
5c83 int n;
427e //xor fwt : A[i] = \sigma{-1^([i&j])*a[j]}   [x]:count of 1-bit
3284 void FWT(int *a,int n,int r){
65de     for (int i=1;i<n;i<<=1){
2d6f         for (int j=0;j<n;j+=(i<<1)){
3d77             for (int k =0;k<i;k++){
269d                 int x = a[j+k];int y = a[j+k+i];
f418                 if (r){
a62b                     a[j+k] = (x+y)%MOD;
df0f                     a[j+k+i] = (x-y+MOD)%MOD;
8e2e                 }else{
a36d                     a[j+k] = 1LL*(x+y)*INV2%MOD;
5b23                     a[j+k+i] = 1LL*(x-y+MOD)*INV2%MOD;
95cf                 }
95cf             }
```

```
95cf        }
95cf    }
95cf }
e854 LL pow_mod(LL x,LL y){
1938     LL ret = 1;
4fc6     for (;y;y>>=1){if (y&1) ret = ret*x%MOD;x = x*x%MOD;}
ee0f     return ret;
95cf }
3117 int main(){
cd91     scanf("%d",&n);
6dbf     for (int i=1;i<=n;i++){
7681         int x;scanf("%d",&x);
52fe         a[x]++;
95cf     }
564e     FWT(a,N,1);
8cc2     for(int i=0;i<N;i++){
788a         a[i] = (n+2*a[i])%MOD;
2be0         int cnt3 = 1LL*(a[i]+n)%MOD*INV4%MOD;
c3f6         int cnt1 = n-cnt3;
557b         a[i] = pow_mod(3,cnt3);
9f4a         if (cnt1&1)a[i] = MOD-a[i];
95cf     }
e16f     FWT(a,N,0);
369d     printf("%d\n",(a[0]+MOD-1)%MOD);
7021     return 0;
95cf }
```

7.3 BerlekampMassey

```
427e // Created by calabash_boy on 18-8-16.
302f #include<bits/stdc++.h>
d196 #define FOR(i,l,r) for (int i = (l);i<(r);i++)
ba3e #define FORD(i,r,l) for (int i= (r);i>(l);i--)
421c using namespace std;
5cad typedef long long LL;
7c77 typedef vector<LL> V;
b575 const int MOD = 1e9+7;
427e // k 为 m 最高次数 且 a[m] == 1
70d2 namespace BerlekampMassey {
a44f     inline void up(LL& a, LL b) { (a += b) %= MOD; }
427e
68c4     V mul(const V& a, const V& b, const V& m, int k) {
138d         V r; r.resize(2 * k - 1);
4c60         FOR (i, 0, k)
d87c             FOR (j, 0, k)
01e3                 up(r[i + j], a[i] * b[j]);
43e8         FORD (i, k - 2, -1) {
d87c             FOR (j, 0, k)
bbda                 up(r[i + j], r[i + k] * m[j]);
57fc             r.pop_back();
95cf         }
547e         return r;
95cf     }
e854     LL pow_mod (LL x,LL y){
1938         LL ret =1;
4fc6         for (;y;y>>=1){if (y&1) ret = ret*x%MOD;x = x * x %MOD;}
ee0f         return ret;
95cf     }
025b     LL get_inv(LL x,LL MOD){
a4c6         return pow_mod(x,MOD-2);
95cf     }
b35e     V pow(LL n, const V& m) {
737d         int k = (int)m.size() - 1; assert(m[k] == -1 || m[k] == MOD - 1);
bd5c         V r(k), x(k); r[0] = x[1] = 1;
ddfe         for (; n; n >>= 1, x = mul(x, x, m, k))
77c0             if (n & 1) r = mul(x, r, m, k);
547e         return r;
95cf     }
0d21     LL go(const V& a, const V& x, LL n) {
427e         // a: (-1, a1, a2, ..., ak).reverse
427e         // x: x1, x2, ..., xk
427e         // x[n] = sum[a[i]*x[n-i],{i,1,k}]
84ec         int k = (int)a.size() - 1;
f0f5         if (n <= k) return x[n - 1];
4690         V r = pow(n - 1, a);
f7ff         LL ans = 0;
4c60         FOR (i, 0, k)
d862             up(ans, r[i] * x[i]);
4206         return ans;
95cf     }
427e
ad3d     V BM(const V& x) {
89e6         V a = {-1}, b = {233};
c493         FOR (i, 1, x.size()) {
73f7             b.push_back(0);
6453             LL d = 0, la = a.size(), lb = b.size();
```

```
            FOR (j, 0, la) up(d, a[j] * x[i - la  + 1 + j]);
            if (d == 0) continue;
            V t; for (auto& v: b) t.push_back(d * v % MOD);
            FOR (j, 0, a.size()) up(t[lb - 1 - j], a[la - 1 - j]);
            if (lb > la) {
                b = a;
                LL inv = -get_inv(d, MOD);
                for (auto& v: b) v = v * inv % MOD;
            }
            a.swap(t);
        }
        for (auto& v: a) up(v, MOD);
        return a;
    }
    void sample();
}
void BerlekampMassey::sample(){
    V x(6);
    x[0] = 1;x[1] = 2;
    x[2] = 21;x[3] = 212;
    x[4] = 2141;x[5] = 21622;
    V a = BerlekampMassey::BM(x);
    cout<<"a[n]=";
    for (int i = 0;i<a.size()-2;i++){
        cout<<a[i]<<"*a[n-"<<a.size()-1-i<<"]+";
    }
    cout<<a[a.size()-2]<<"*a[n-1]"<<endl;
}
int main(){
    BerlekampMassey::sample();
    return 0;
}
```

7.4 CRT

```
//
// Created by DELL on 2019/2/12.
//luogu 4777
#include<bits/stdc++.h>
using namespace std;
typedef long long ll;
const int maxn = 1e5+100;
namespace CRT{
    ll ex_gcd(ll a,ll b,ll& x,ll& y){
        if (b == 0){x = 1;y = 0;return a;}
        ll gcd = ex_gcd(b,a%b,x,y);
        ll t = x;x = y;y = t - a/b*y;
        return gcd;
    }
    ll mul_mod(ll a,ll b,ll m){
        ll res = 0;
        while (b){
            if (b&1){
                res = (res + a) % m;
            }
            b >>=1;
            a = a * 2 % m;
        }
        return res;
    }
    // ans = first + t * second;
    // x = second (mod first)
    pair<ll,ll>work(vector<pair<ll,ll> >&es ){
        ll ans = es[0].second;
        ll M = es[0].first;
        for (int i=1;i<es.size();i++){
            ll a = es[i].first;
            ll b = es[i].second;
            ll x,y;
            ll gcd = ex_gcd(M,a,x,y);
            ll c = (b - ans %a + a) % a;
            a/=gcd;
            if (c % gcd)return {-1,-1};
            x = (mul_mod(x ,(c / gcd),a) + a)% a;
            ans += M * x;
            M *= a;
            ans %= M;
        }
        return {ans,M};
    }
}
vector<pair<ll,ll> > es;
int main(){
    int n;
    scanf("%d",&n);
    for (int i=0;i<n;i++){
```

```
        ll a,b;
        scanf("%lld%lld",&a,&b);
        es.push_back(make_pair(a,b));
    }
    pair<ll,ll> ans = CRT::work(es);
   // cout<<ans.first<<" "<<ans.second<<endl;
    ll x = ans.first;
    cout<<x<<endl;
    return 0;
}
```

7.5 Linear Sieve

```
#include<bits/stdc++.h>
using namespace std;
const int maxn = 1e7+10;
typedef long long ll;
bool used[maxn];
int mu[maxn];
vector<int> prime;
ll f[maxn];
int low[maxn];
void sieve(int size){
    //f:multiplicative function;
    assert(size < maxn);
    mu[1] = 1;
    f[1] = 1;
    for (int i=2;i<=size;i++){
        if (!used[i]){
            prime.push_back(i);
            mu[i] = -1;
            //f:TODO
            low[i] = i;
        }
        for (int j = 0;j < prime.size();j++){
            ll nxt = 1ll * i * prime[j];
            if (nxt > size)break;
            used[nxt] = 1;
            if (i % prime[j]){
                low[nxt] = prime[j];
                mu[nxt] = -mu[i];
                //f: mod or not?
                f[nxt] = f[i] * f[prime[j]];
            }else{
                low[nxt] = prime[j] * low[i];
                mu[nxt] = 0;
                if (low[nxt] != nxt){
                    //mod or not?
                    f[nxt] = 1ll * f[low[nxt]] * f[nxt/low[nxt]];
                }else{
                    // i = prime[j] ^ k
                    //f:TODO
                }
                break;
            }
        }
    }
}
int main(){
    sieve(1e7);
    return 0;
}
```

7.6 Linear Basis

```
/* Generated by powerful Codeforces Tool
 * Author: calabash_boy_love_15
 * Time: 2019-05-15 11:00:02
 * Personal Code Template: https://github.com/4thcalabash/ACM-Code-Library
**/
#include <bits/stdc++.h>
using namespace std;
int s[maxn];
int n;
struct Linear_Basis{
    //basis vector
    int basis[22];
    //basis vector in origin data
    int num[22];
    void clear(){
        memset(basis,0,sizeof basis);
        memset(num,0,sizeof num);
    }
    void ins(int x){
```

```
c7a6         int bk = x;
54c0         for (int i=20;i>=0;i--){
a0f3             if (x & (1<< i)){
e222                 if (!basis[i]){basis[i] = x;num[i] = bk;break;}
370c                 x ^= basis[i];
95cf             }
95cf         }
95cf     }
5bcc     int count(){
8abb         int cnt = 0;
9f1c         for (int i=0;i<=20;i++){
340e             cnt += (basis[i] != 0);
95cf         }
6808         return cnt;
95cf     }
56dd     void debug(){
af23         _debug("basis␣:␣");
9f1c         for (int i=0;i<=20;i++){
dbf5             if (basis[i])_debug("%d␣:␣%d",i,basis[i]);
95cf         }
95cf     }
4a42 }basis;
3117 int main(){
e1b6     cin>>n;
6dbf     for (int i=1;i<=n;i++){
f9af         cin>>s[i];
9f1c         basis.ins(s[i]);
95cf     }
7021     return 0;
95cf }
```

7.7 Mobius

```
e9ac /* x in [1,N]; y in [1,M] (x,y) = 1 */
59b9 #include<cstdio>
09f7 #include<vector>
421c using namespace std;
52c1 const int maxn = 1e5+100;
4085 typedef long long ll;
727f bool used[maxn];
7c8f vector<int> prime;
a00a ll mu[maxn];
9bc6 void sieve(){
7f5a     mu[1] = 1;
82c4     for (int i=2;i<maxn;i++){
efb1         if(!used[i]){
1024             prime.push_back(i);
7171             mu[i] = -1;
95cf         }
eb1a         for (int j = 0;j<prime.size();j++){
b70b             long long nxt = 1ll* prime[j] * i;
1487             if(nxt >= maxn)break;
6b89             used[nxt] = 1;
20cc             if (i % prime[j] == 0){
8ec3                 mu[nxt] = 0;
6173                 break;
8e2e             }else{
66f9                 mu[nxt] = -mu[i];
95cf             }
95cf         }
95cf     }
95cf }
8399 ll work(int n,int m){
19f3     ll ans = 0;
78fb     int top = min(n,m);
3d1c     for (int i=1;i<=top;i++){
7d55         ans += 1ll * mu[i] * (n/i) * (m/i);
95cf     }
4206     return ans;
95cf }
3117 int main(){
5ec4     sieve();
9523     int T;
1fd9     scanf("%d",&T);
9415     for (int Case = 1;Case <= T;Case ++){
fb8b         int a,b,n,m,k;
cc1c         scanf("%d%d%d%d%d",&a,&n,&b,&m,&k);
5399         if(k == 0){
8acc             printf("Case␣%d:␣0\n",Case);
b333             continue;
95cf         }
0dac         n/=k;
a94f         m/=k;
0d4c         printf("Case␣%d:␣%lld\n",Case,work(n,m) - work(min(n,m),min(n,m))/2);
95cf     }
7021     return 0;
```

```
}
```

8 Others

8.1 Header

```
// Created by calabash_boy
#pragma GCC optimize(3)
#include <bits/stdc++.h>
using namespace std;
#ifdef __LOCAL_DEBUG__
# define _debug(fmt, ...) fprintf(stderr, "\033[91m[%s␣%3d]:␣" fmt "\n\033[0m",
  \
  __func__,__LINE__, ##__VA_ARGS__)
#else
# define _debug(...) (void(0))
#endif
#define PB(x) push_back(x)
#define rep(i,l,r) for (int i = l,_ = r;i< _;i++)
#define REP(i,l,r) for (int i=l,_=r;i<=_;i++)
#define leave(x) do {cout<<#x<<endl;fflush(stdout);return 0;}while (0);
#define untie do{ios::sync_with_stdio(false);cin.tie(nullptr);cout.tie(nullptr)
  ;}while (0)
#define range(x) x.begin(),x.end()
typedef long long LL;
typedef long long ll;
typedef vector<int> vi;
typedef vector<ll> vl;
typedef long double db;
typedef pair<int,int> pii;
typedef pair<ll,ll> pll;
const int inf = 0x3f3f3f3f;
const ll inf_ll = 0x3f3f3f3f3f3f3f3fLL;
mt19937 wdy(time(0));
/************* header ******************/
int main(){
    return 0;
}
```

8.2 FORMULA

```
C(n,m)%2 = (n&m)==m
约瑟夫问题：
F(n,m) = 有n个人(0,1,2,..,n-1)，每次杀掉编号为(x + m) %n的人，最终的幸存者。
F(n,m) = (F(n-1,m) + m ) % n
```